

Full Bridge Inverter (Single Phase) –  
Autonomous Square Wave Operation (50 Hz)

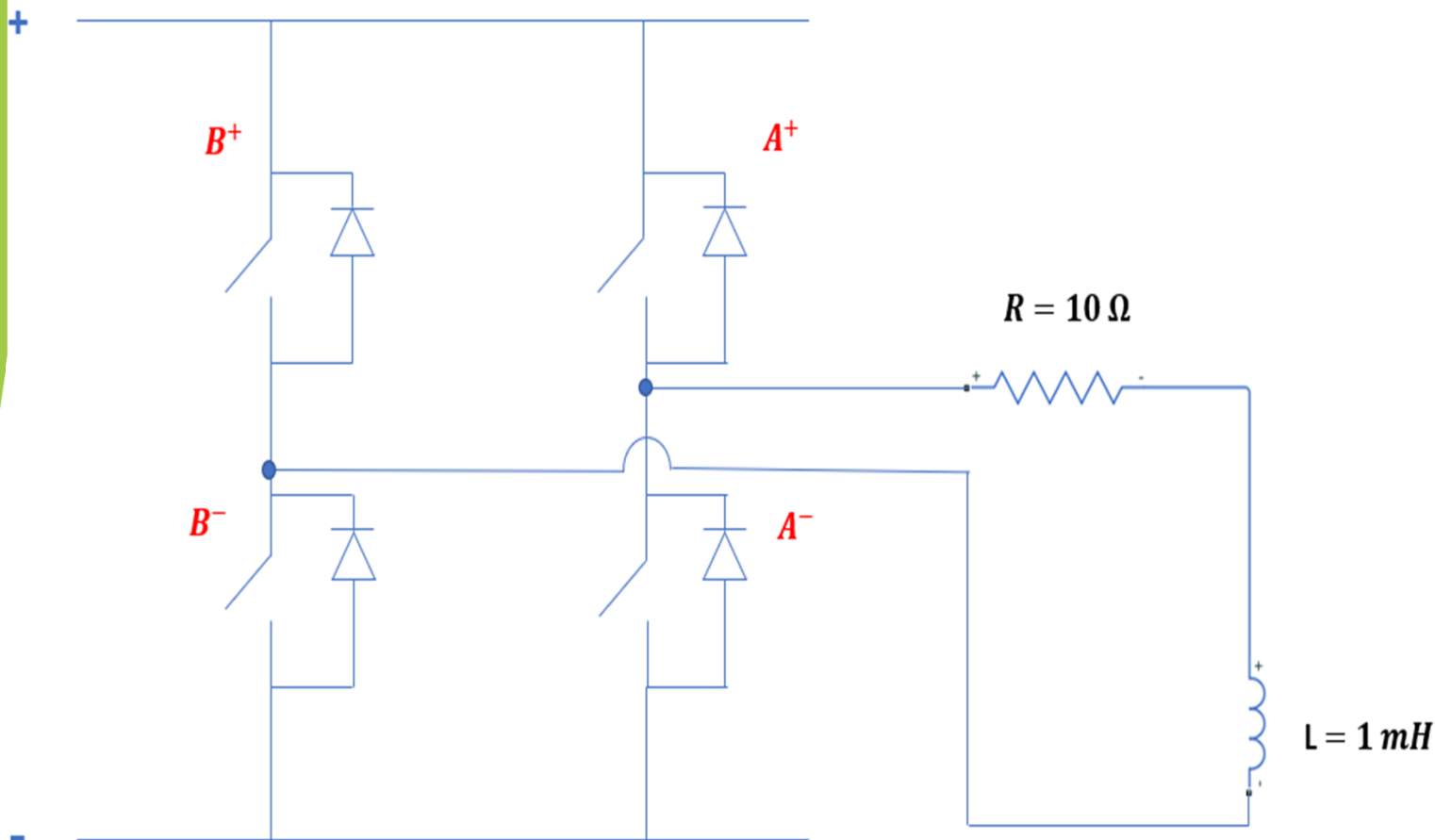
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# Theory

- ▶ Full bridge inverter is a topology of H-bridge inverter used for converting DC power into AC power. The components required for conversion are two times more than that used in single phase Half bridge inverters. The **circuit of a full bridge inverter** consists of 4 diodes and 4 controlled switches as shown below.
- ▶ The general concept of a full bridge inverter is to alternate the polarity of voltage across the load by operating two switches at a time. Positive input voltage will appear across the load by the operation of T1 and T2 for a half time period. The polarity of voltage across load will be changed for the other half period by operating T3 and T4.

The circuit arrangement for the full-bridge inverter is shown in Figure.



$$V_o^2 = \frac{2}{T_o} \int_0^{T_o/2} V_s^2 dt = \frac{2}{T_o} V_s^2 \frac{T_o}{2}$$

$$\Rightarrow V_o = V_s$$

$$V_{o,n} = \frac{4V_s}{\sqrt{2}n\pi} = \frac{2\sqrt{2}V_s}{n\pi}$$

$$\Rightarrow V_{o,n} = \frac{4V_s}{n\pi} \sin n \omega t$$

$$n = 1, 3, 5, \dots$$

i) Calculate the  $V_s$ , when  $V_{o,s} = 230 V$

$$V_{o,s} = \frac{4V_s}{\sqrt{2\pi}} = \frac{2\sqrt{2}V_s}{\pi} \Rightarrow V_s = \frac{\pi V_{o,s}}{2\sqrt{2}} = \frac{3,14 \cdot 230}{2\sqrt{2}} = 255,3 V$$

ii) Calculate the active, reactive, and the apparent power at 50 Hz

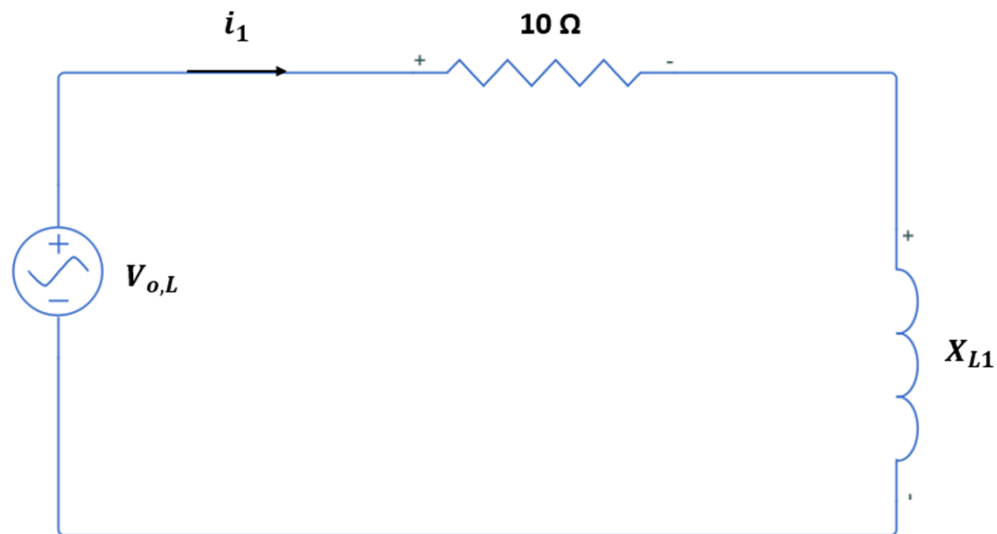
$$I_{1,rms} = \frac{V_{o,L}}{\sqrt{R^2 + X_{L1}^2}} = 23 A$$

$$P_1 = I_{rms}^2 \cdot R = 5290 W$$

$$Q_1 = I_{rms}^2 \cdot X_{L1} = 166 VAR$$

$$S_1 = \sqrt{P_1^2 + Q_1^2} = 5293 VA$$

$$X_{L1} = 2\pi f 1mH = 0,314 \Omega$$



iii) Calculate the  $THD_v$  (%)

$$THD_v = \frac{V_{oH,rms}}{V_{o,s}} \cdot 100\% = \frac{\sqrt{V_o^2 - V_{o,s}^2}}{V_{o,s}} \cdot 100\% = \sqrt{\left(\frac{V_o}{V_{o,s}}\right)^2 - 1} \cdot 100\% = 47,9 \%$$

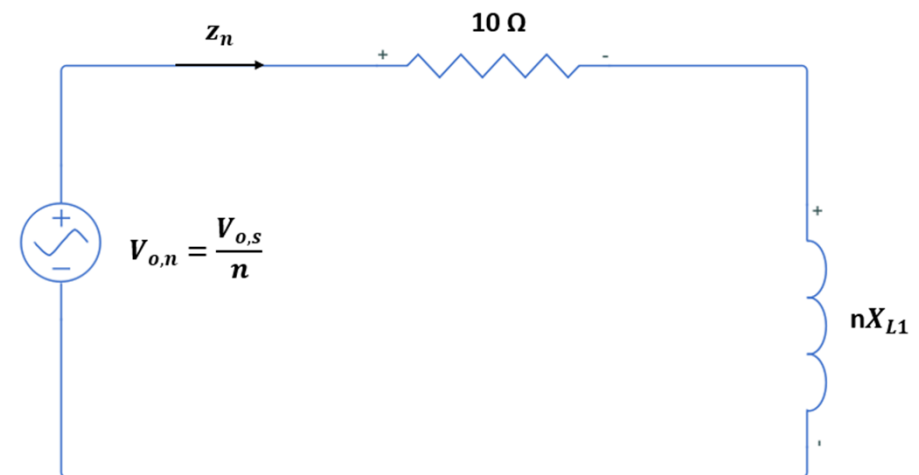
iv) Calculate the  $THD_i$  (%) for  $n_{max} = 21$ .

➤ n- 50 Hz Equivalent Circuit

$$I_{n,rms} = \frac{V_{o,n}}{\sqrt{R^2 + X_{Ln}^2}} = \frac{V_{o,s}}{n \sqrt{R^2 + X_{L1}^2}}$$

$$I_{o,rms H} = \left[ \sum_{n=3}^{21} I_{n,rms}^2 \right]^{1/2} = 10,4 \text{ A}$$

$$THD_i (\%) = \frac{I_{o,H}}{I_{o,s}} \cdot 100\% = 45,2 \%$$



$$I_{3,rms} = 7,7 \text{ A}$$

$$I_{5,rms} = 4,5 \text{ A}$$

$$I_{7,rms} = 3,2 \text{ A}$$

$$I_{9,rms} = 2,5 \text{ A}$$

$$I_{11,rms} = 2 \text{ A}$$

$$I_{13,rms} = 1,6 \text{ A}$$

$$I_{15,rms} = 1,4 \text{ A}$$

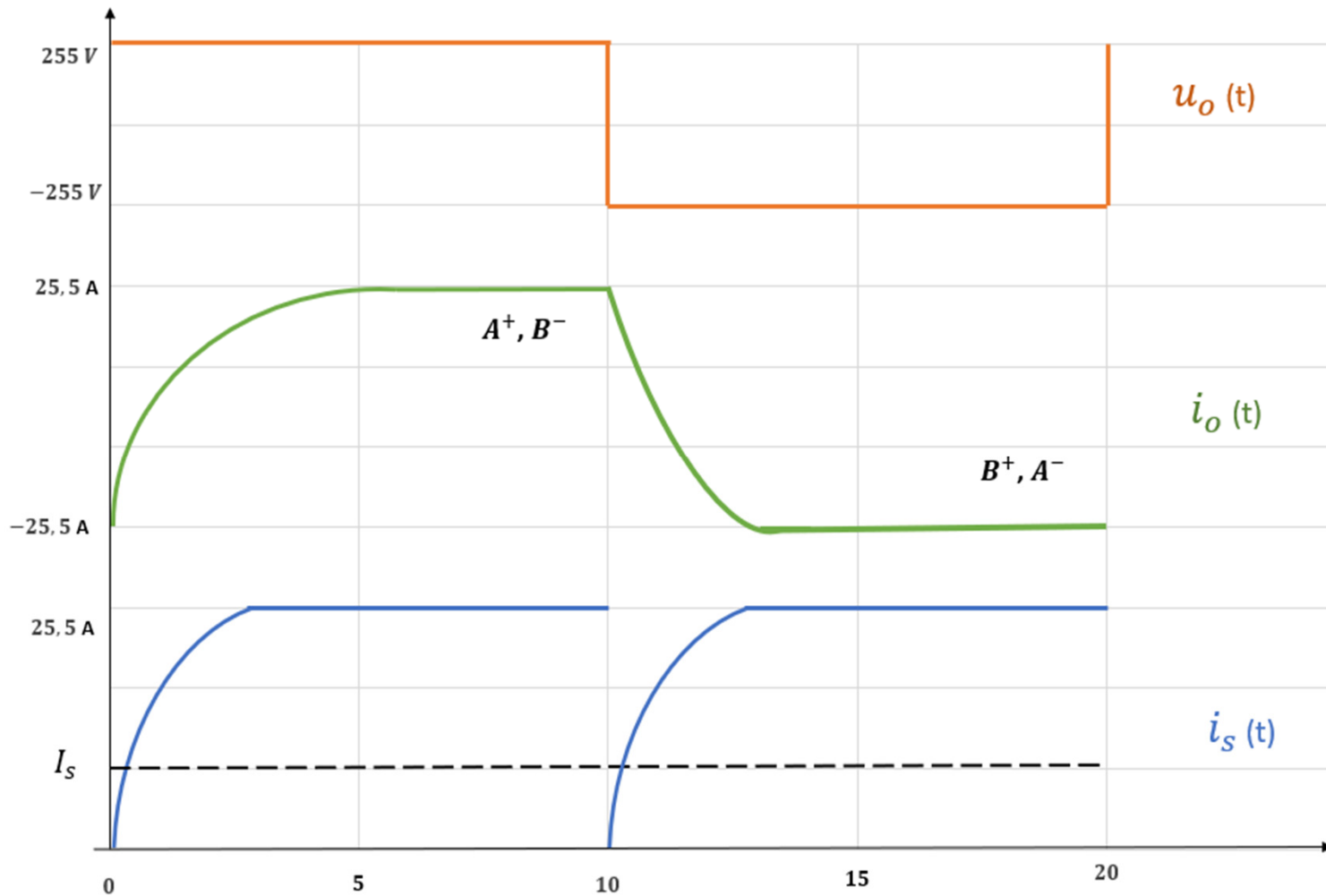
$$I_{17,rms} = 1,2 \text{ A}$$

$$I_{19,rms} = 1 \text{ A}$$

$$I_{21,rms} = 0,1 \text{ A}$$

## v) Calculate $u_o(t), i_o(t), i_s(t)$

Figure shows the voltage and current waveforms in the circuit.



►  $z = \frac{L}{R} = \frac{1\text{m}}{10} \text{ sec} = 0,1 \text{ msec}$

►  $I_p = \frac{V_s}{R} = 25,5 \text{ A}$

vi) Calculate the  $I_s$

$$I_{o,rms} = \sqrt{I_{os,rms}^2 + I_{oH,rms}^2} = 25,2 \text{ A}$$

$$P_o = I_{o,rms}^2 \cdot R = 6350,4 \text{ W}$$

$$P_o = V_s \cdot I_s \Rightarrow I_s = \frac{P_o}{V_s} = 24,9 \text{ A}$$