



μ μ

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μμ

2



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μ

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$(Q_m):$

μ μ (μ , μ , μ , μ).

$(Q_{min}):$

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μ μ μ

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$\mu\mu$

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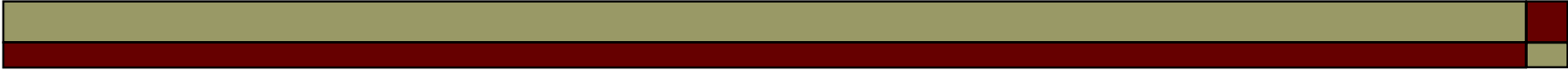
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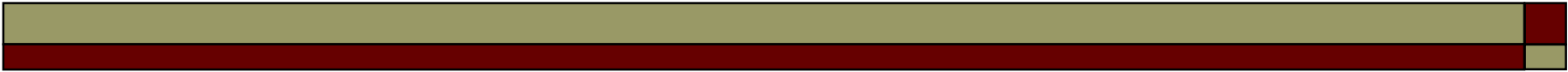
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μ :

□ μ

■ $\mu \mu$ (mm),

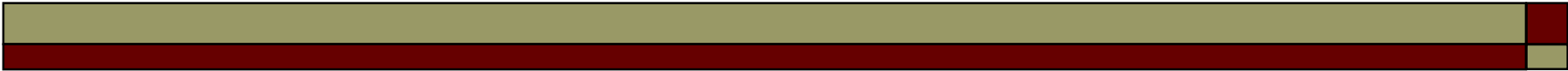
■ (24),

■ μ

■ μ .

□ μ

□ ()



μ

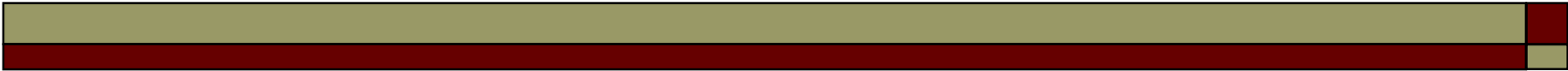
μ μ

μ
μ

(2000 ~ 2600m).

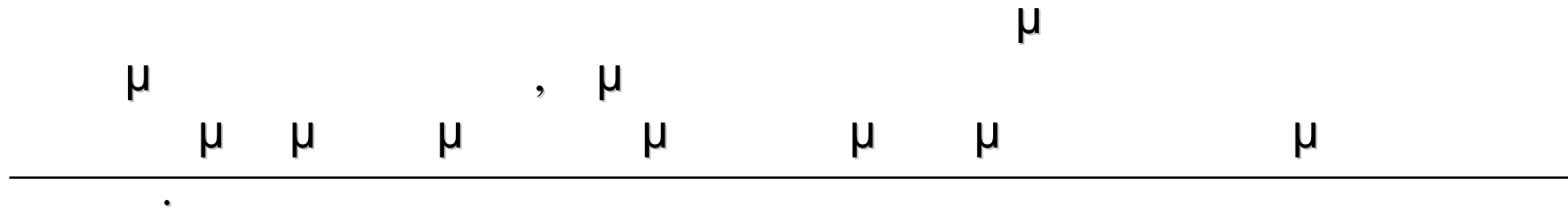
μ

	(mm/100m)
	50
	65
	112
	35
	55
	96
	125



(μ % μ μ).

(m)	(%)
500	10
1000	20
1500	34
2000	51
2500	68
3000	85



□

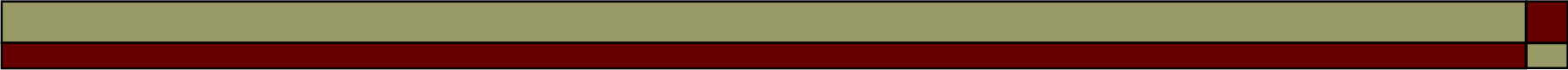
Mathias

$$N_H = \cdot H - \frac{1}{2} \cdot \left(\frac{H^2}{100} \right)$$

□

Wussow

$$N_H = 44 + \sqrt{44^2 + H^2 - 80 \cdot H}$$



24 ()

μ , μ
 μ μ ()
):

$$N_{24} = 15,6 + 0,012 \cdot H \quad (\text{mm}/24\text{h})$$

μ
 μ μ . μ
 μ μ μ μ

(Flocas et al., 1983):

$$T = - (\cdot) - (\cdot) - (\cdot)$$

, , , μ μ μ (m)



(
 μ), μ μ μ μ μ
 μ , μ μ μ μ μ
 μ : μ

$$\bar{T} = \bar{\mu} \cdot \quad (C)$$

:
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 (C)
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μ



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$$\bar{T}_E = 28,5 + 0,002 \cdot H$$

,

μ

μ

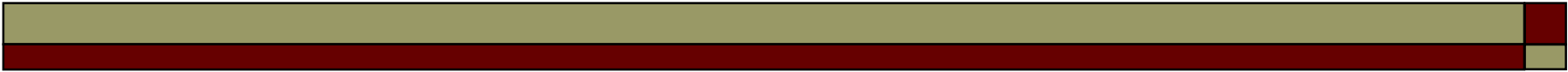
μ

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μ

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$$T_{,E} = T_{o,E} + 0,002 \cdot \Delta H$$



μ μ μ

μ μ , μ
 μ μ μ μ μ μ μ
 μ μ . μ μ μ μ μ

■ *Turc*

$$ET = \frac{\mu}{\sqrt{0,9 + \left(\frac{\mu}{L}\right)^2}} \quad (\text{mm})$$

L: μ μ (mm)
 μ ,

$$L = 300 + 25 \cdot T + 0,05 \cdot T^3 \quad (\text{mm})$$

μ (°C)

■ *Coutagne*

$$ET = \left(1 - \frac{\mu}{\mu_0}\right) (mm)$$

$$\mu = \mu_0 \cdot ET \quad (\mu, \mu_0 \text{ (mm)})$$

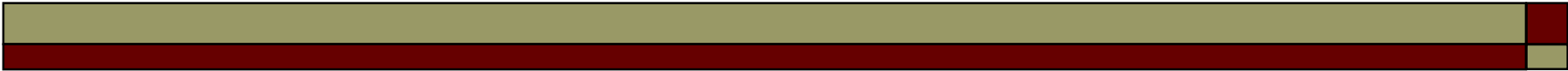
$$I = 800 + 140 \cdot T \quad (\text{mm})$$

$$T = \frac{I - 800}{140} \quad (C)$$

$$\frac{I}{8} \leq N \leq \frac{I}{2}$$

$$\begin{aligned} &< /8, & \cong & \mu \\ &> /2, & \cong & /4 = 200 + 35 \cdot \mu \end{aligned}$$

(μ , μ_0) Turc, Coutagne (μ).



(μ)

μ μ μ μ μ μ μ μ .
μ μ μ
:

μ	(%)
	20 ~ 25
	10 ~ 25
	4 ~ 8
, , , , .	3 ~ 8
	5 ~ 12
, μμ , .	14 ~ 25
μ	3 ~ 8
, , μ	3 ~ 7



μ

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μ

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μ

□

μ

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μ

μ

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□

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μ

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μ

$\mu\mu$

μ

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μ

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□

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μ

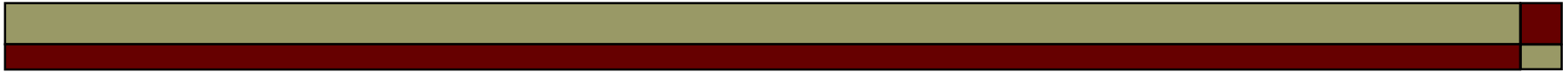
μ

μ

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2



□ $\mu\mu$:

μ μ μ

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□ :

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$\mu\mu$

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μ μ

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(μ ,)

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1.

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(μ t),

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2.

μ

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(

μ μ t_M)

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μ

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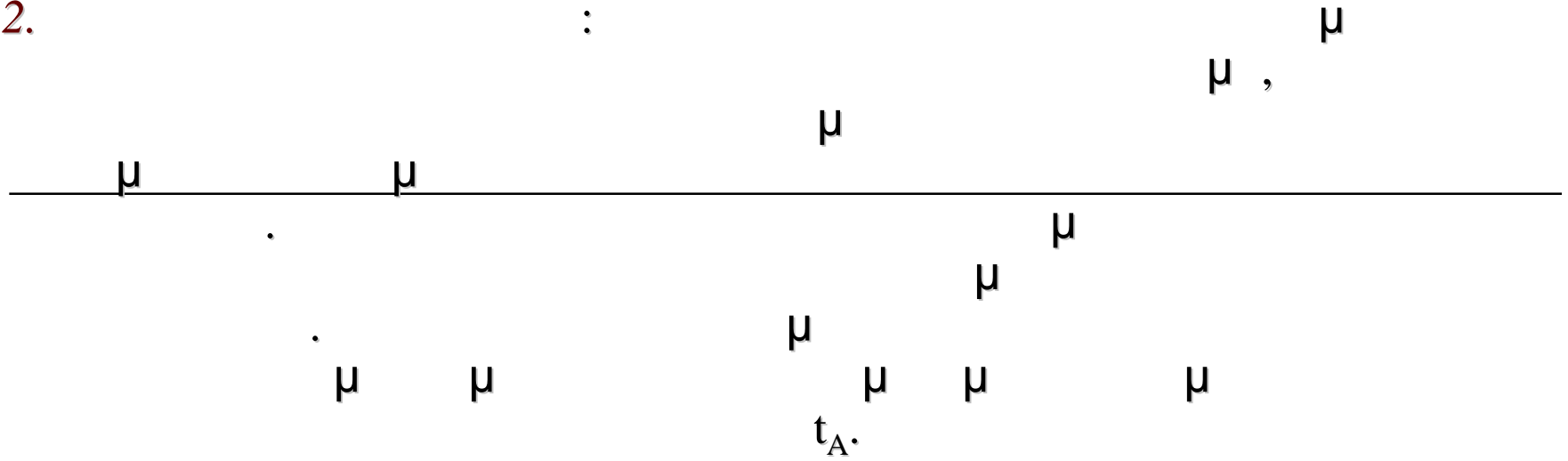
.

$(t_{AS} = t_B + t_M)$

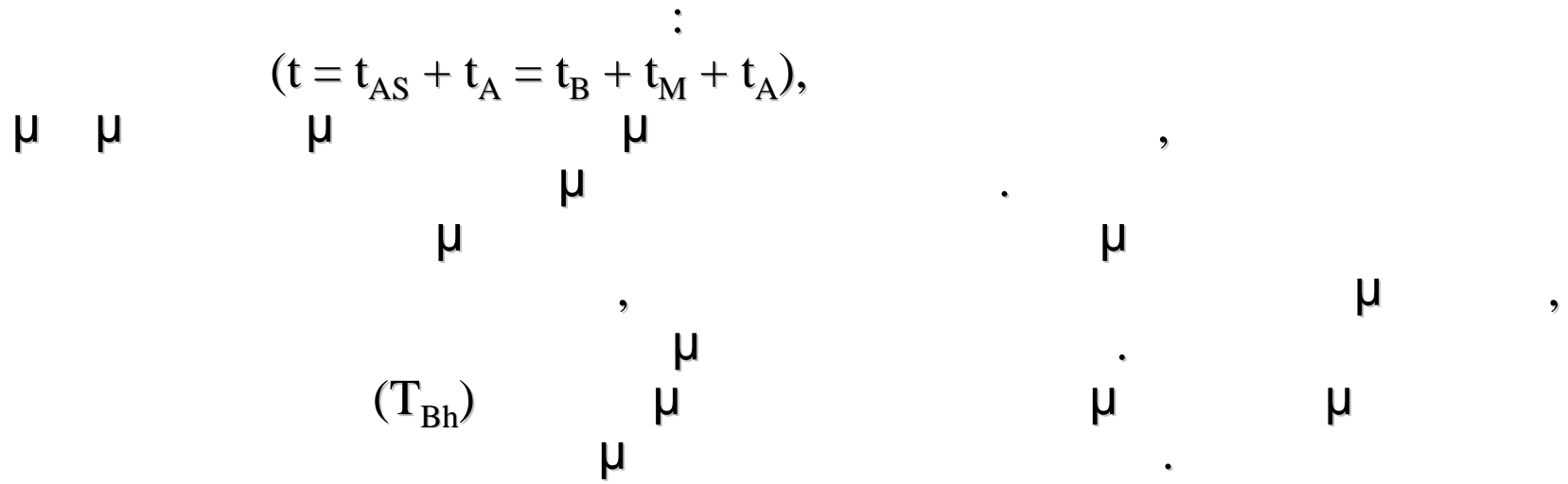
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2.

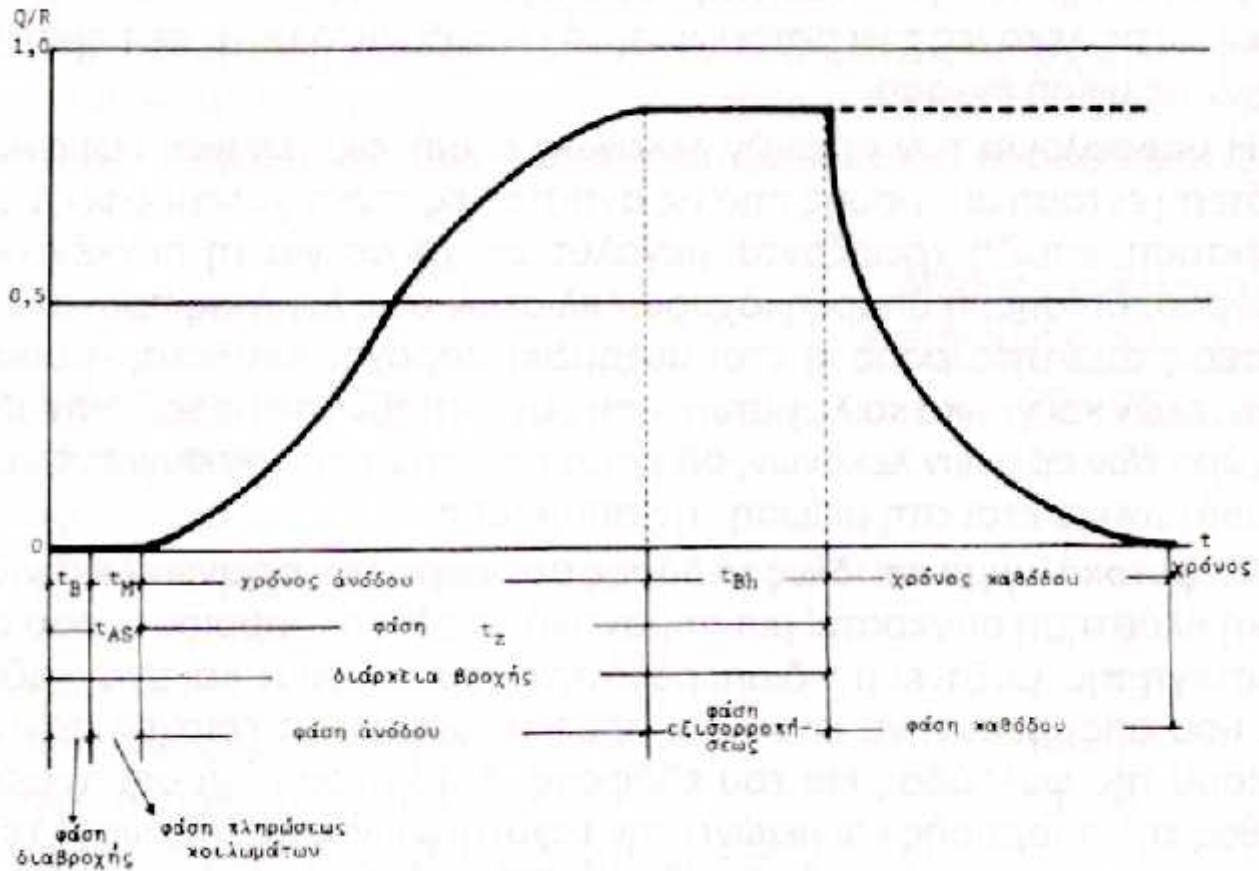


3.



4.

μ
 μ
 (t_{Ab})





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3.

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 μ μ μ μ μ
m/s) μ , μ (μ μ μ 3 ~ 4
: μ :

$$Q = 1,90 \cdot b \cdot h^{3/2}$$

Q: (m³/s)

b: (m)

μ : b_o : (m)

B_u : (m)

h: (m)

μ : μ μ 0,60 ~ 0,65

$$Q = 1,90 \cdot b \cdot h^{3/2} \cdot \frac{3 \cdot b_o + 2 \cdot b_u}{5}$$

4.

μ

μ

μμ

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μ μ

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μ

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Manning – Strickler:

$$u = k \cdot J^{1/2} \cdot R^{3/2}$$

u: μ

(m/s)

J:

μ

μμ

,

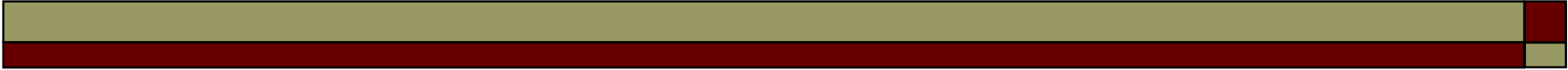
R:

(m)

k:

:

$$Q = F \cdot u \quad (m^3/s)$$



4.

μ μ

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μ
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μ μ
 μ μ



μ μ μ

$(Q_{\max 100})$

μ

$(Q_{\max N})$

μ

μ

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μ

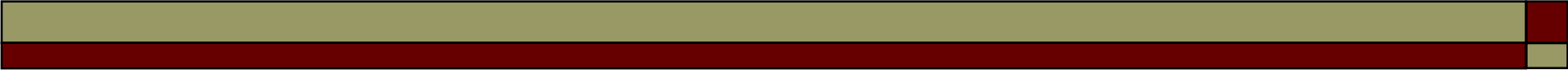
$\mu\mu$

μ (μ , μ)

μ μ

μ

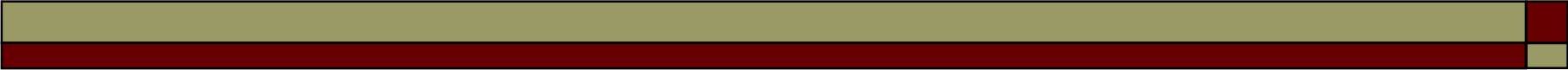
μ μ μ (, ,).



μ ()

μ	()	μ	μ
	F: M		(km ²)
	q: E	(m ³ /s, km ²),	Q = q · F (m³/s)

- $Q_{\max} = 14 \cdot \sqrt{F} \cdot \log_{10} F$ 5 ~ 200 km²
- ***Freidrich*** $Q_{\max} = 24,12 \cdot F^{0,516}$
- ***Klement – Wunderlich*** $Q_{\max} = 5,5 \cdot F^{5/6}$ ()
- ***Wundt*** $Q_{\max} = 13,8 \cdot F^{0,6}$
- ***Coutagne*** $Q_{\max} = a \cdot F^{1/2}$ (a = 0,6 ~ 2,0)



q: E	F: M	(m³/s, km²),	(km²)	Q = q · F (m³/s)
□ <i>Valentini</i>		$q_{\max} = \frac{30}{F^{1/2}}$		
□ <i>Kürsteirner</i>		$q_{\max} = \frac{A}{F^{2/3}}$	$\mu = 12 \sim 15$	$\mu = 9$
□ <i>Henry Boot</i>		$Q_{\max} = a \cdot F^{0,75}$		μ , $a = 3,3 \sim 6,7$
□ <i>Hoffbauer</i>		$q_{\max} = a \cdot \frac{60}{F^{1/2}}$	μ	$F > 10 \text{ Km}^2$ $a = 0,35 \sim 0,50$ $a = 0,50 \sim 0,70$
□ <i>Melli</i>		$q_{\max} = a \cdot \frac{40}{(100 \cdot F)^{1/6}}$		$F < 150 \text{ Km}^2$, $a = 0,4$ (μ μ)

$q: E$ $F: M$ (km^2)
 $(m^3/s, km^2),$ $Q = q \cdot F (m^3/s)$

Kresnik $q_{max} = a \cdot \frac{32}{0,5 + F^{1/2}}$ $a = 0,6 \sim 2,0$

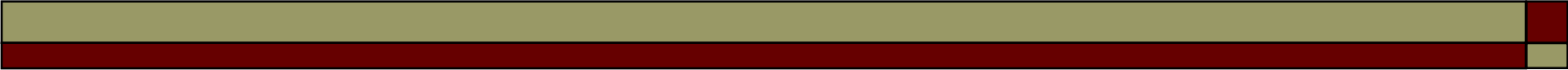
Müller $q_{max} = y_m \cdot \frac{40}{F^{1/3}},$ $y_m = \frac{F_1 \cdot y_1 + F_2 \cdot y_2}{F}$

F_1

F_2

y_1, y_2

	,	0,4	0,6	0,8
		0,2	0,4	0,6
μ	,	0,1	0,2	0,4



q: E **F: M** (km²)
 (m³/s, km²) , **Q = q · F (m³/s)**

□ **Meli – Müller**

$$Q_{\max} = y \cdot 43 \cdot F^{2/3}$$

	y
	0,4 ~ 0,8
μ	0,05 ~ 0,4
	0,3 ~ 0,6
	0,2 ~ 0,5
	0,1 ~ 0,5
	0,05 ~ 0,4

$\mu \mu$

$$y_m = \frac{\sum_i y_i \cdot \Delta F_i}{\sum_i \Delta F_i} \quad Q_{\max} = y_m \cdot 43 \cdot F^{2/3}$$

> 50 % y_m

1,1

< 20 % y_m

0,9

$q: E$ $F: M$ (km^2)
 $(m^3/s, km^2),$ $Q = q \cdot F (m^3/s)$

□ *Iszkowski* $q_{max} = ah \cdot m \cdot H$

$ah:$ (μ) , $> 1000 \text{ mm}$
 $m:$ μ

F:	1	10	20	50	100	500
m:	10	9,5	9,0	7,95	7,40	5,90

	I	II	III	IV
μ , ,	0,030	0,055		
, μ	0,035	0,050	0,125	
	0,04 ~ 0,05	0,082 ~ 0,140	0,155 ~ 0,29	0,4 ~ 0,55
	0,06 ~ 0,08	0,16 ~ 0,21	0,36 ~ 0,60	0,60 ~ 0,80

$V:$ μ μ μ
 μ μ μ μ

q: E **F: M** **(km²)**
(m³/s, km²), **Q = q · F (m³/s)**

□ **Possenti** $Q_{\max} = \frac{a \cdot I_N}{L} \cdot \left(E_H + \frac{E_N}{3} \right)$

a: 700 (μ)
 L: μ μ μ (Km)
 E_N, E_H: (km²)

□ $Q_{\max} = 0,278 \cdot c \cdot i \cdot F$

c:
 i: (mm/h)

q: E **F: M** (km²)

(m³/s, km²), **Q = q · F (m³/s)**

□ **Fuller**

$$\max Q_N = Q_1 \cdot (1 + \mu \cdot \log_{10} T) \cdot \left(1 + \frac{2,66}{F^{0,30}} \right)$$

Q₁: μ μ (m³),

$$Q_1 = 1,80 \cdot F^{0,8}$$

: 0,8

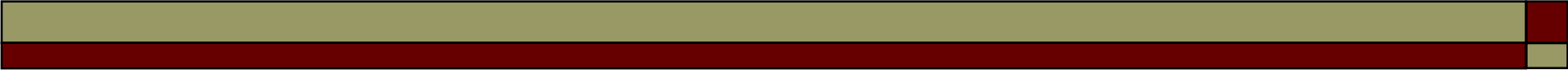
:

()	1	5	10	20
1+0,8	1,00000	1,55920	1,80000	2,04080
	30	40	50	100
	2,18168	2,28168	2,35920	2,60000



- *Turazza*

- *Giandotti*



, a: (μ)

: μ , =2

t_p: μ t_p=t_c
 t_c: μ (μ)

$$t_c = \frac{t'_c}{24}, \quad t'_c = t_c \cdot \mu$$

$$t'_c = \frac{4 \cdot \sqrt{F} + 1,5 \cdot L}{0,8 \cdot \sqrt{Z}} \quad ()$$

L: (Km)

Z: μ μ μ (m)

h_p: μ μ t_p (m)

$$h_p = \frac{h'}{1000}$$

$$Q_{\max(100)} = 11,57 \cdot a \cdot K \cdot F \cdot \frac{h_p}{t_p + t_c}$$

h': μ t'_p (mm)

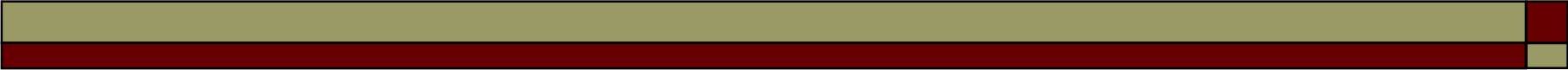
$$h' = \left[a - \left(\frac{a}{72} t'_p \right) \right] \cdot \sqrt{t'_p}$$

a:

$$a = \frac{h}{3,27}$$

t'_p: t_p

h: 24/



P:

t'c (mm)

Giandotti

$$P = h \cdot \sqrt{\frac{t'_c}{24}}$$

h: μ

24/ (mm)

$$Q_{\max} = \frac{0,277 \cdot P \cdot F}{t'_c}$$

t'c: μ

$$t'_c = \frac{4 \cdot \sqrt{F} + 1,5 \cdot L}{0,8 \cdot \sqrt{Z}} \quad (\quad)$$

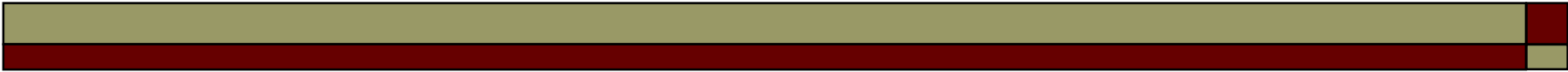
L: μ

(Km)

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μ μ

μ (m)



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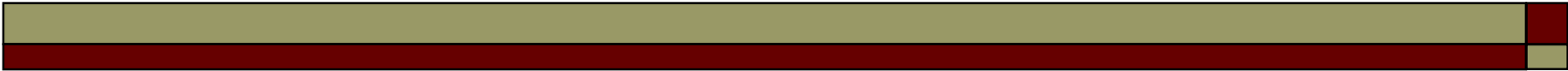
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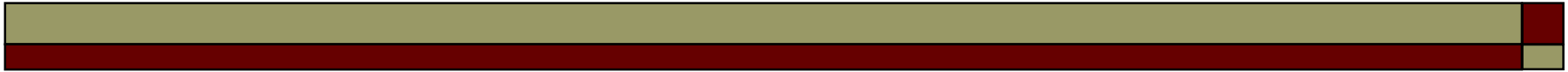
μ

μ **μ**

$(Q = \mu)$).



μ **μ** **μ** **μ** ($Q =$)
 $\mu\mu$ (J_e), μ (J_w)
 μ (J_s) , **$J_e = J_w = J_s$** ,
 $\mu\mu$ μ μ ,
 μ , μ μ μ .
 μ μ ,
 μ , ,
 μ μ
 μ **μ** **μ**
 ,



μ

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:

μ

$$u_m = \frac{Q}{U}$$

Q: (m³/sec)

U: μ (m²)



Manning - Strickler

$$u_m = k \cdot R^{2/3} \cdot J^{1/2}$$

k: ()

R:

J: μ



μ

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($J_s > 5 \sim 10\%$),

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(α) υποκρίσιμη (ποτάμια) ροή



(β) υπερκρίσιμη (χειμαρρώδης) ροή

2.

$\mu \mu$

$\mu , :$

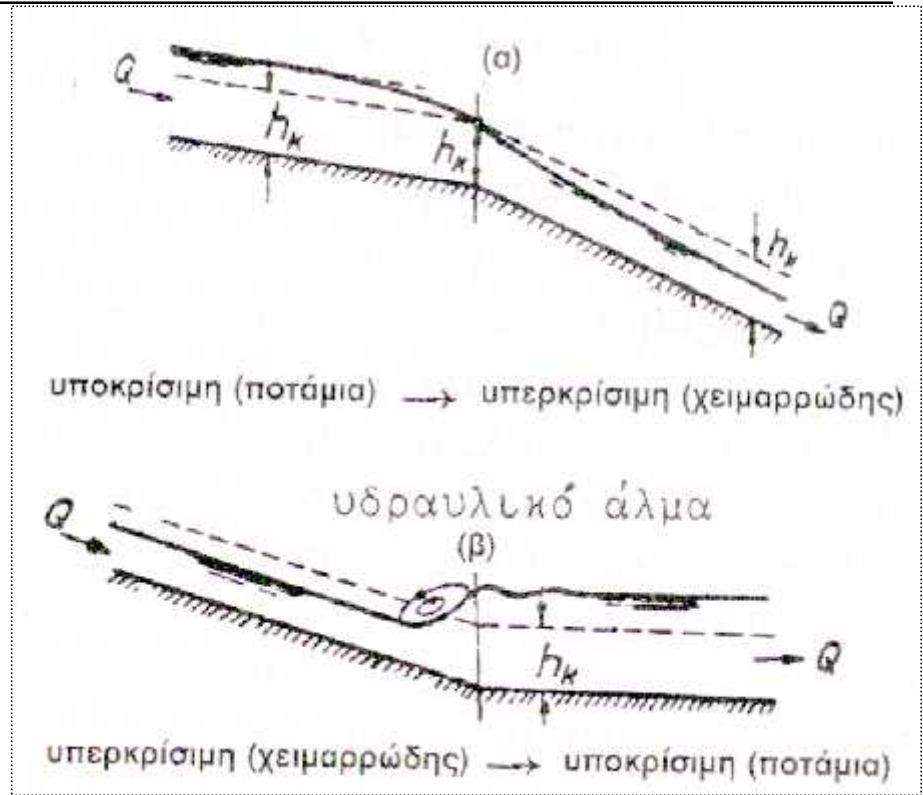
□

$\mu (\mu) \mu (\mu)$
 $\mu (\mu) \mu (\mu)$
 $\mu (\mu) \mu (\mu)$

μ , μ
 $\mu)$

□

μ , μ
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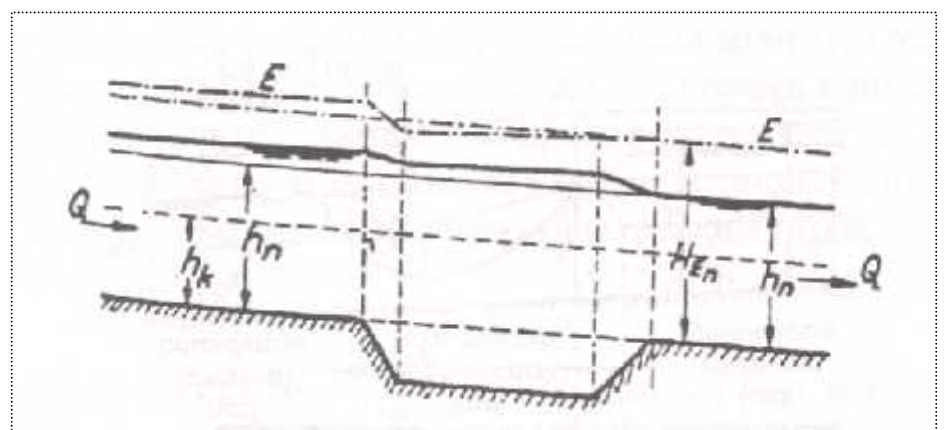
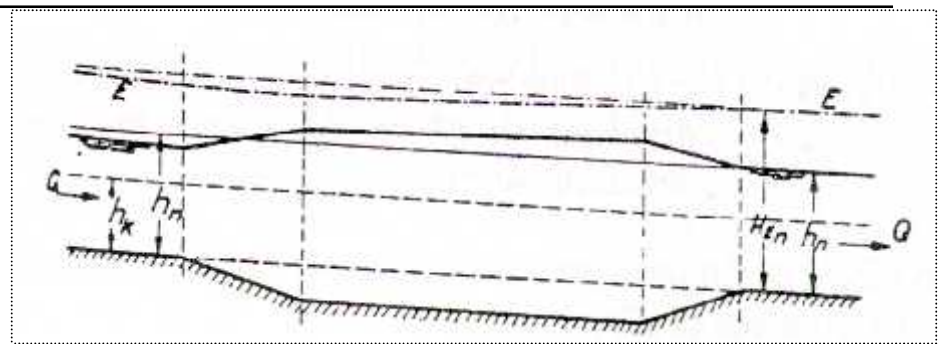




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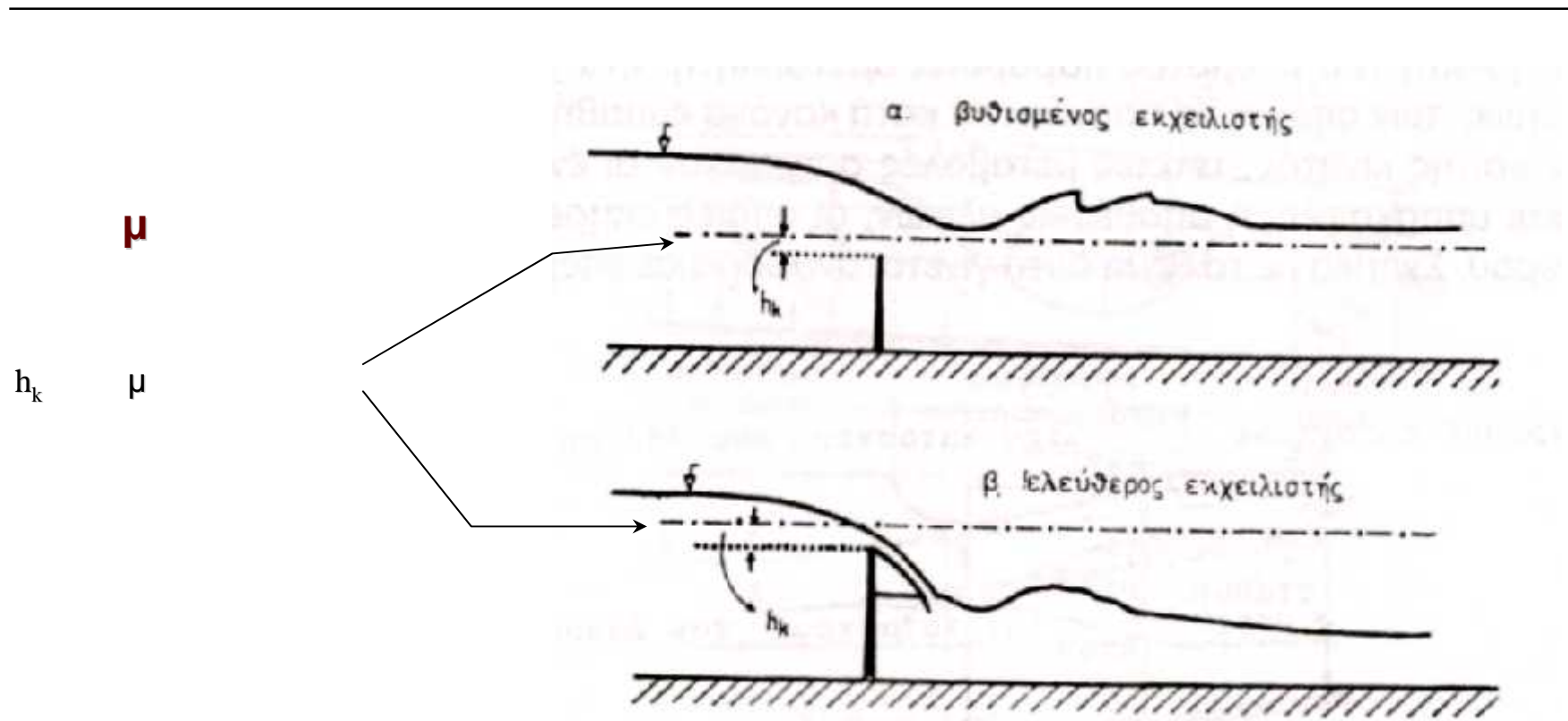
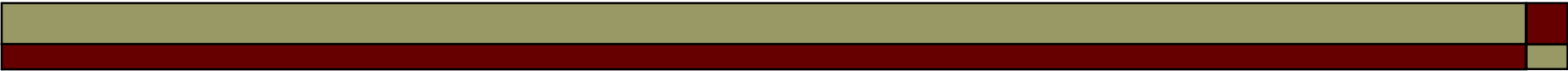
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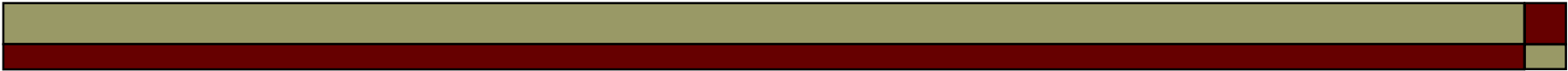
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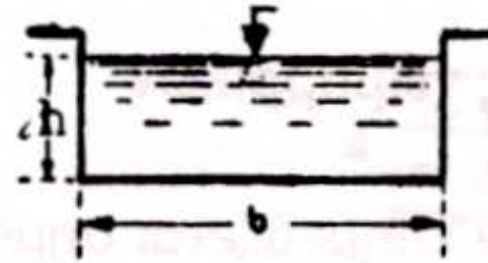




μ
,
μ (μ)
μ μ μ μ μ
(Manning – Strickler).

$$u_m = k \cdot R^{2/3} \cdot J^{1/2}$$

(μ)



μ

Weissbach,

$$Q = \frac{2}{3} \cdot \mu \cdot b \sqrt{2g} \left[\left(h + \frac{u^2}{2g} \right)^{3/2} - \left(\frac{u^2}{2g} \right)^{3/2} \right]$$

Q: (m³/sec)

b: (m)

g: (m²/sec)

h: (m)

u: (m/s)

μ : , μ , μ

$$\mu = 0,60 \sim 0,65.$$

2,5 ~ 3,0 m/s), μ , μ ($u <$
Poleni: μ

$$Q = \frac{2}{3} \cdot \mu \cdot b \sqrt{2g} \cdot h^{3/2}$$

μ μ ,
 μ μ μ ,
 Poleni μ μ μ $\mu = 0,60 \sim 0,65,$
 μ μ :

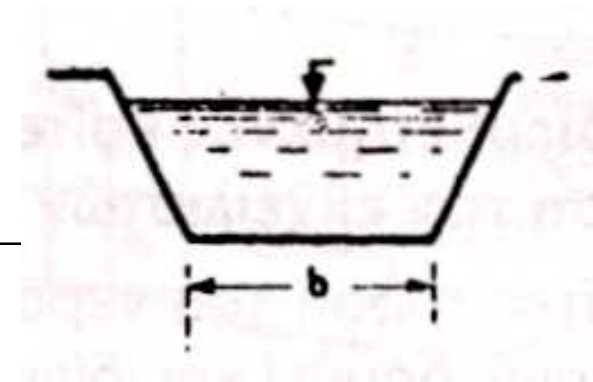
$$Q = 1,70 \cdot b \cdot h^{3/2}$$

μ μ .

(μ)

μ

Weissbach.



$$Q = \frac{2}{3} \cdot \mu \cdot \sqrt{2g} \cdot \left[\left(b_u + \frac{b_o - b_u}{h} \cdot h \right) \cdot \left(H^{3/2} - h_o^{3/2} \right) - \frac{2}{5} \cdot \frac{b_o - b_u}{h} \cdot \left(H^{5/2} - h_o^{3/2} \right) \right]$$

Q: (m³/sec)

b_u: (m)

b_o: (m)

H: H = h + h_o (m)

g: (m²/sec)

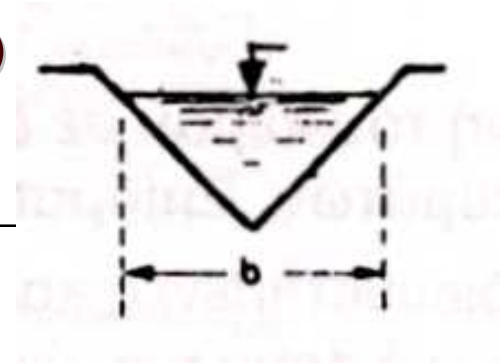
h: (m)

h_o: h_o = u²/2g

u: (m/s)

μ : , $\mu = 0,60 \sim 0,65.$

(Thomson)



$$Q = 0,553 \cdot \mu \cdot \sqrt{2g} \cdot h^{5/2}$$

: , μ , μ
 , μ
 2 μ
 h: (m)
 = 45 () μ μ
 h.

h:	0,05	0,1	0,15	0,2	0,25
μ :	0,597	0,590	0,586	0,584	0,582

$$Q = \frac{2}{3} \cdot \mu \cdot \sqrt{2g} \cdot b \cdot h^{3/2}$$

• ειδική παροχή

$$Q = \frac{2}{3} \cdot \mu \cdot \sqrt{2g} \cdot h^{3/2}$$

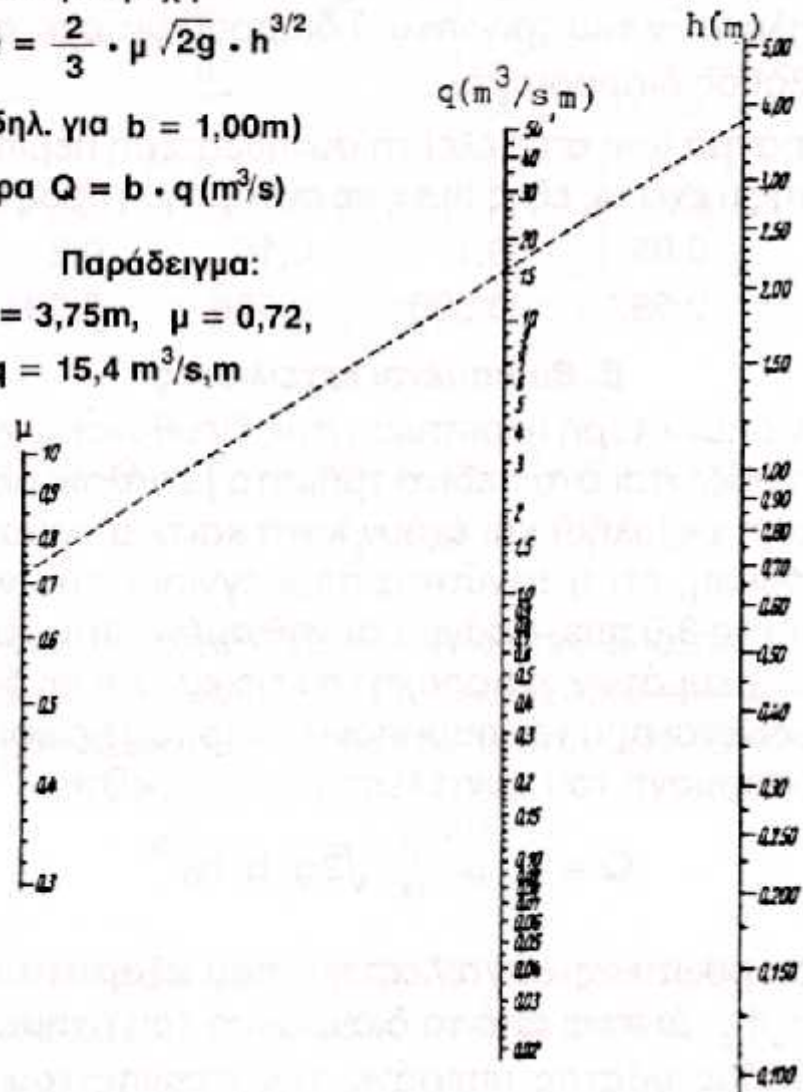
(δηλ. για $b = 1,00\text{m}$)

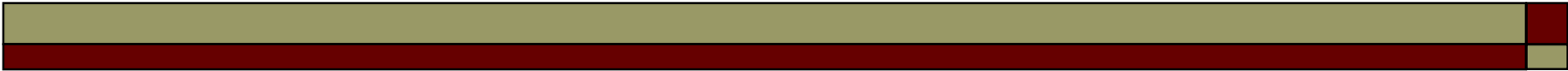
• άρα $Q = b \cdot q \text{ (m}^3/\text{s)}$

Παράδειγμα:

$$h = 3,75\text{m}, \quad \mu = 0,72,$$

$$q = 15,4 \text{ m}^3/\text{s,m}$$





μ



μ μ μ μ ()
 ,
 μ .
 μ *Poleni*, μ μ .

$$Q = c \cdot \frac{2}{3} \cdot \mu \cdot \sqrt{2g} \cdot b \cdot h^{3/2}$$

c

, .

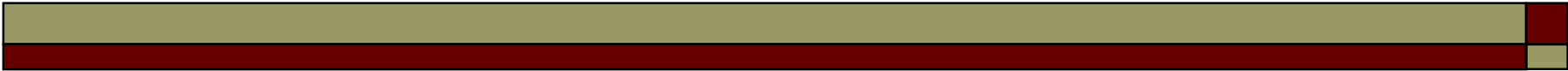


μ



$$z = u \cdot \sqrt{\frac{2h}{g}}$$

z: (m)
 u: μ (m/sec)
 g: (9,81 m/sec²)



μ , μ -
 , μ , μ
 .

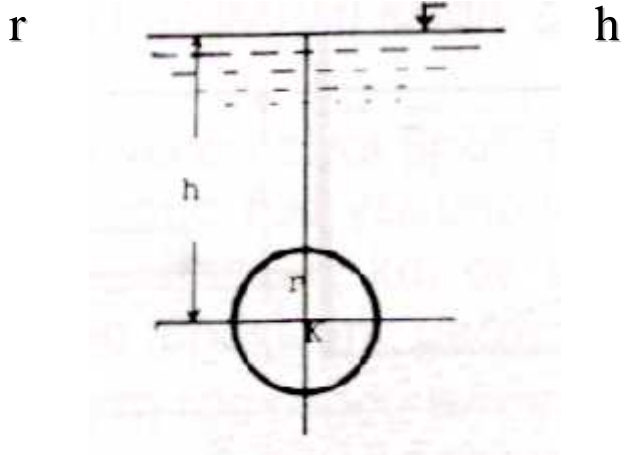
(

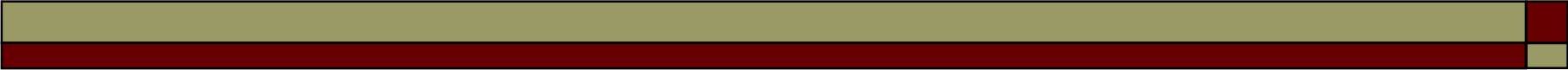
$$Q = 13,9 \cdot \mu \cdot r^2 \cdot \sqrt{h}$$

$r/h > 1/4$
 r: (m)

h: (m)

μ : -





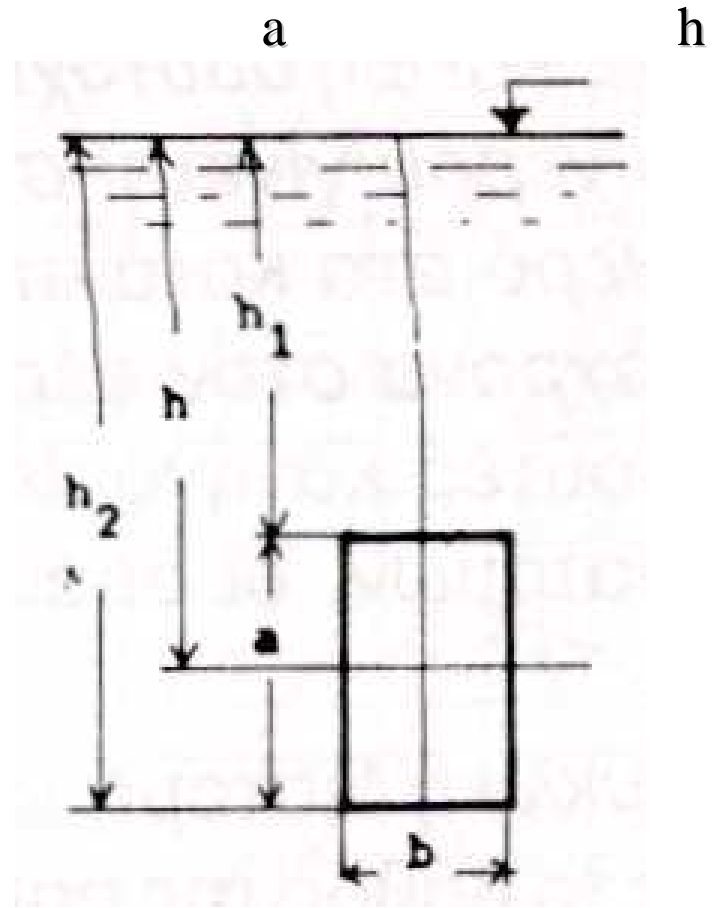
(μ ,
 $h > 2a$)

$$Q = \mu \cdot F \cdot \sqrt{2g \cdot h}$$

F: μ (m²)

h: (m)

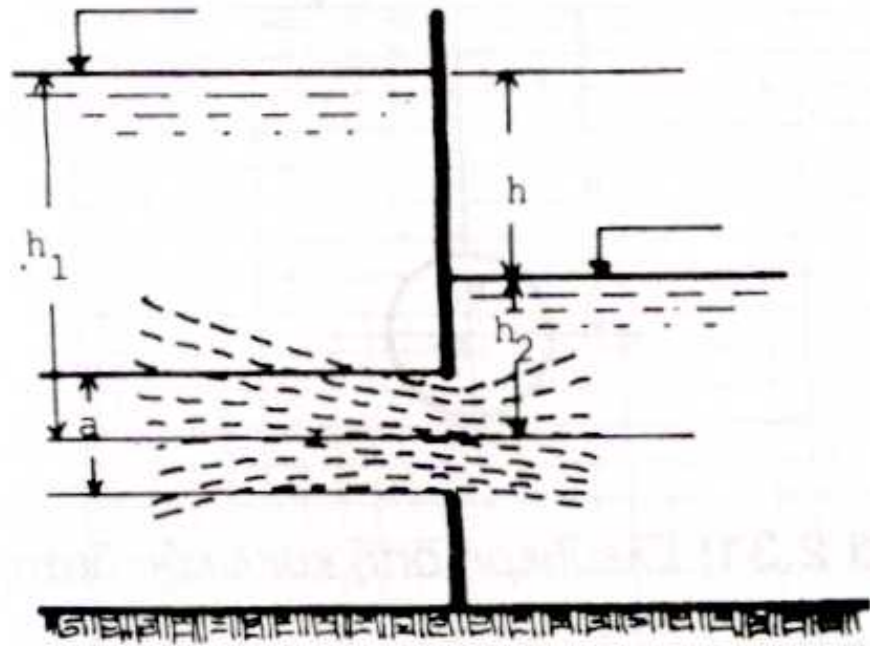
μ :
g: (9,81 m/s²)

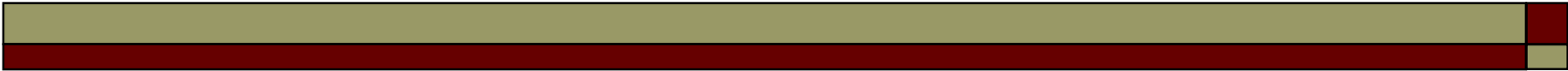


μ

$$Q = \mu \cdot F \cdot \sqrt{2g \cdot h}$$

F: μ (m²)
h: (m)
 μ :
g: (9,81 m/s²)





μ

μ

μ

μ

μ

μ

μ

μ

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μ

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μ

μ

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μ

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μ

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μ

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Darcy:

$$u_f = k_f \cdot J$$

k_f :

(m/s)

J:

μ

μ

μ

μ

$$Q = u_f \cdot f$$

F:

$$Q = k_f \cdot J \cdot F$$

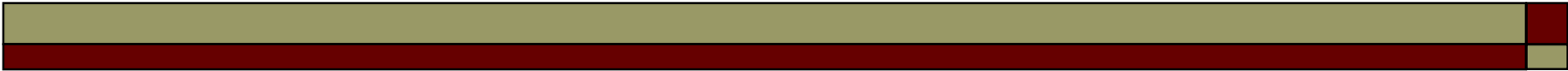
(m²)

k_f

μ

μ

	k_f (cm/s)
$\mu\mu$	0,5 – 1,0
$\mu\mu$	0,1
$\mu\mu$	0,01 – 0,02
	$(0,1 - 1) \cdot 10^{-4}$
	$(0,2 - 20) \cdot 10^{-7}$



μ

- 1.
- 2.
- 3.

