

Τυπολόγιο Μετασχηματισμού Laplace

Συνάρτηση $f: [0, +\infty) \rightarrow \mathbb{R}$	Μετασχηματισμός Laplace $\mathcal{L}[f(t)](s) = F(s) = \int_0^{+\infty} e^{-st} f(t) dt$
1	$\frac{1}{s}, \operatorname{Re}(s) > 0$
t	$\frac{1}{s^2}, \operatorname{Re}(s) > 0$
$t^n, n \in \mathbb{N}^*$	$\frac{n!}{s^{n+1}}, \operatorname{Re}(s) > 0$
$e^{\alpha t}$	$\frac{1}{s - \alpha}, \operatorname{Re}(s) > \alpha$
$te^{\alpha t}$	$\frac{1}{(s - \alpha)^2}, \operatorname{Re}(s) > \alpha$
$\sin(\alpha t)$	$\frac{\alpha}{s^2 + \alpha^2}, \operatorname{Re}(s) > 0$
$e^{\lambda t} \sin(\alpha t)$	$\frac{\alpha}{(s - \lambda)^2 + \alpha^2}, \operatorname{Re}(s) > \lambda$
$\cos(\alpha t)$	$\frac{s}{s^2 + \alpha^2}, \operatorname{Re}(s) > 0$
$e^{\lambda t} \cos(\alpha t)$	$\frac{s - \lambda}{(s - \lambda)^2 + \alpha^2}, \operatorname{Re}(s) > \lambda$
$\sinh(\alpha t)$	$\frac{\alpha}{s^2 - \alpha^2}, \operatorname{Re}(s) > \alpha $
$\cosh(\alpha t)$	$\frac{s}{s^2 - \alpha^2}, \operatorname{Re}(s) > \alpha $
$t^n f(t)$	$(-1)^n F^{(n)}(s)$
$e^{\lambda t} f(t)$	$F(s - \lambda)$
$f(\lambda t)$	$\mathcal{L}[f(\lambda t)](s) = \frac{1}{\lambda} F\left(\frac{s}{\lambda}\right), \lambda > 0, s > c\lambda$
$f'(t)$	$sF(s) - f(0)$
$f''(t)$	$s^2 F(s) - sf(0) - f'(0)$
$f^{(k)}(t)$	$s^k F(s) - s^{k-1}f(0) - \dots - sf^{(k-2)}(0) - f^{(k-1)}(0)$
$\int_0^t f(u) du$	$\frac{1}{s} F(s)$
$f * g(t) = \int_0^t f(u)g(t - u) du$	$F(s) \cdot G(s)$