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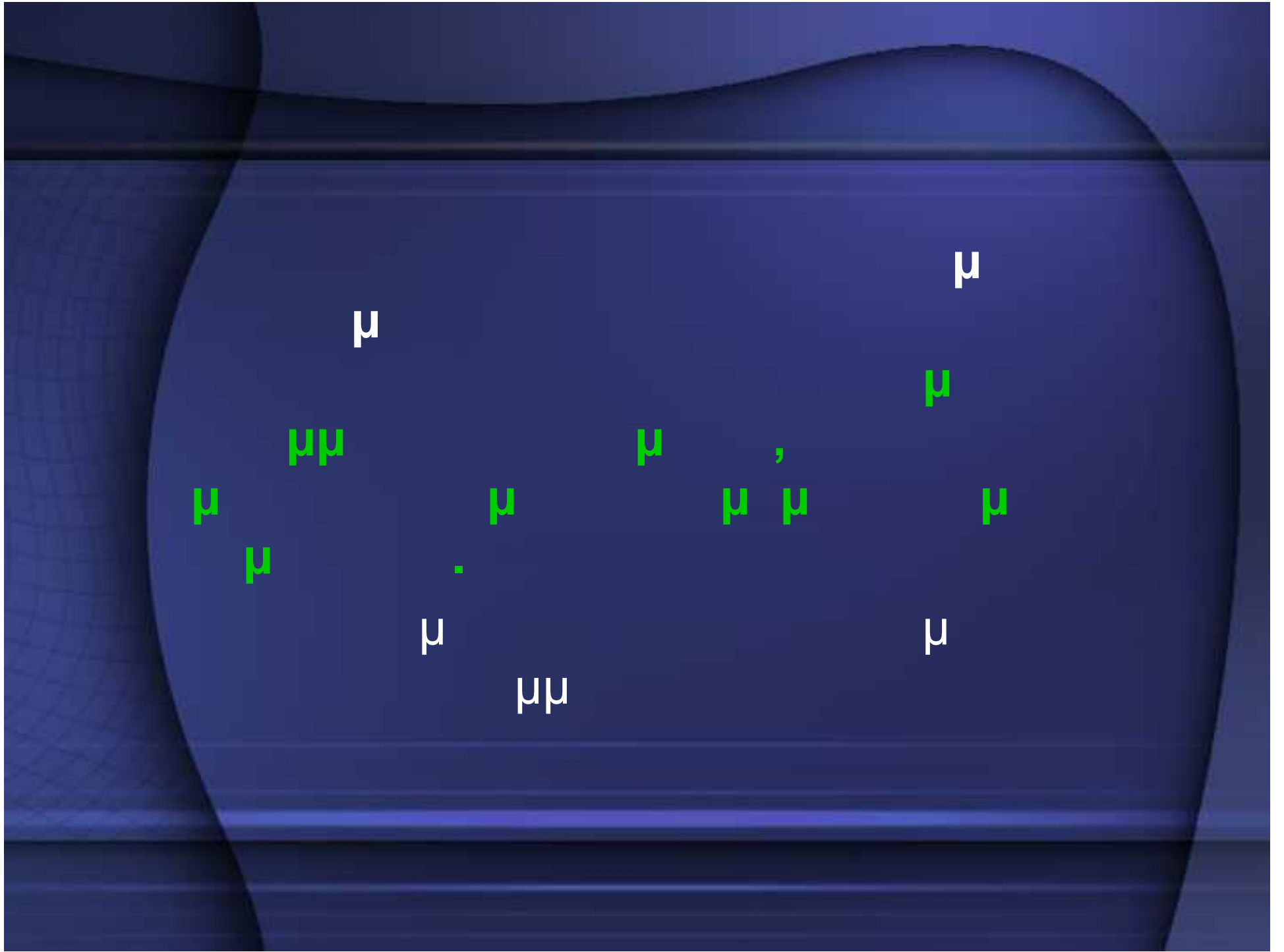


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$A, Q_A(t), Q_B(t)$
 $Q_A(t)$
 $Q_B(t)$

1. $\mu\mu$ μ
- 2.
- 3.
4. $\mu\mu$

$$\max Q_A(t) > \max Q_B(t) \quad (7.1)$$

$$T_B(A) < T_B(B) \quad (7.2)$$

$$\max Q_A \leftarrow t_A < t_B \rightarrow \max Q_B \quad (7.3)$$

$$V_A = \int Q_A dt = \int Q_B dt = V_B \quad (7.4)$$

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μ μ μ μ μ

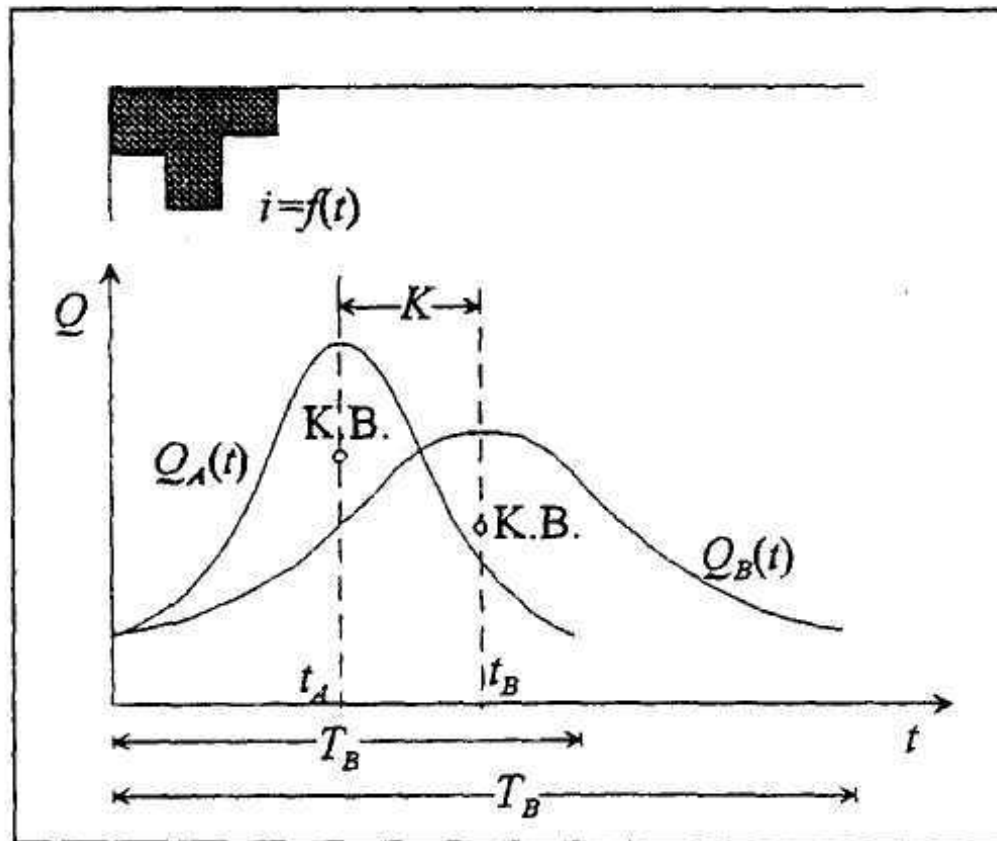
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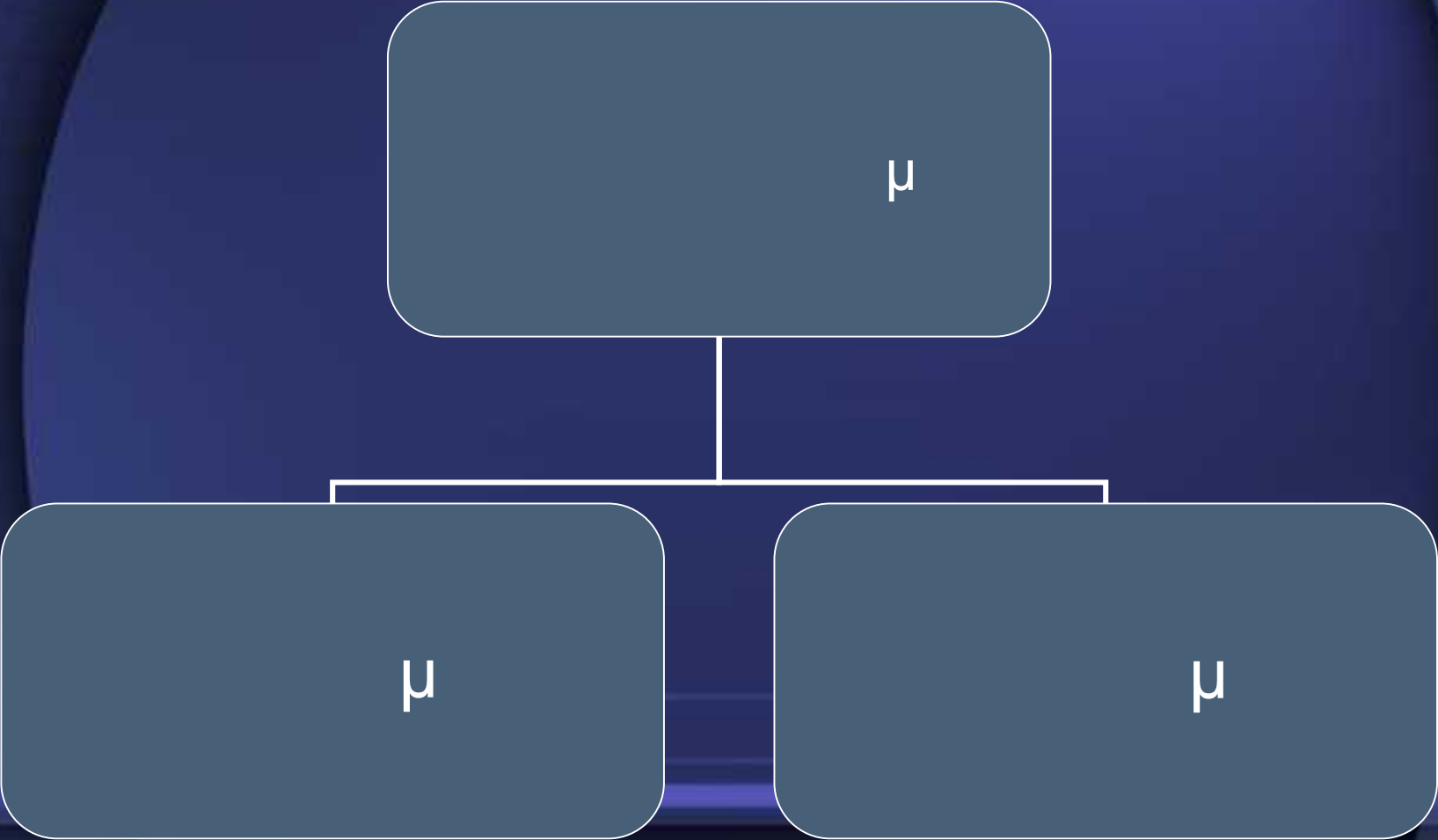
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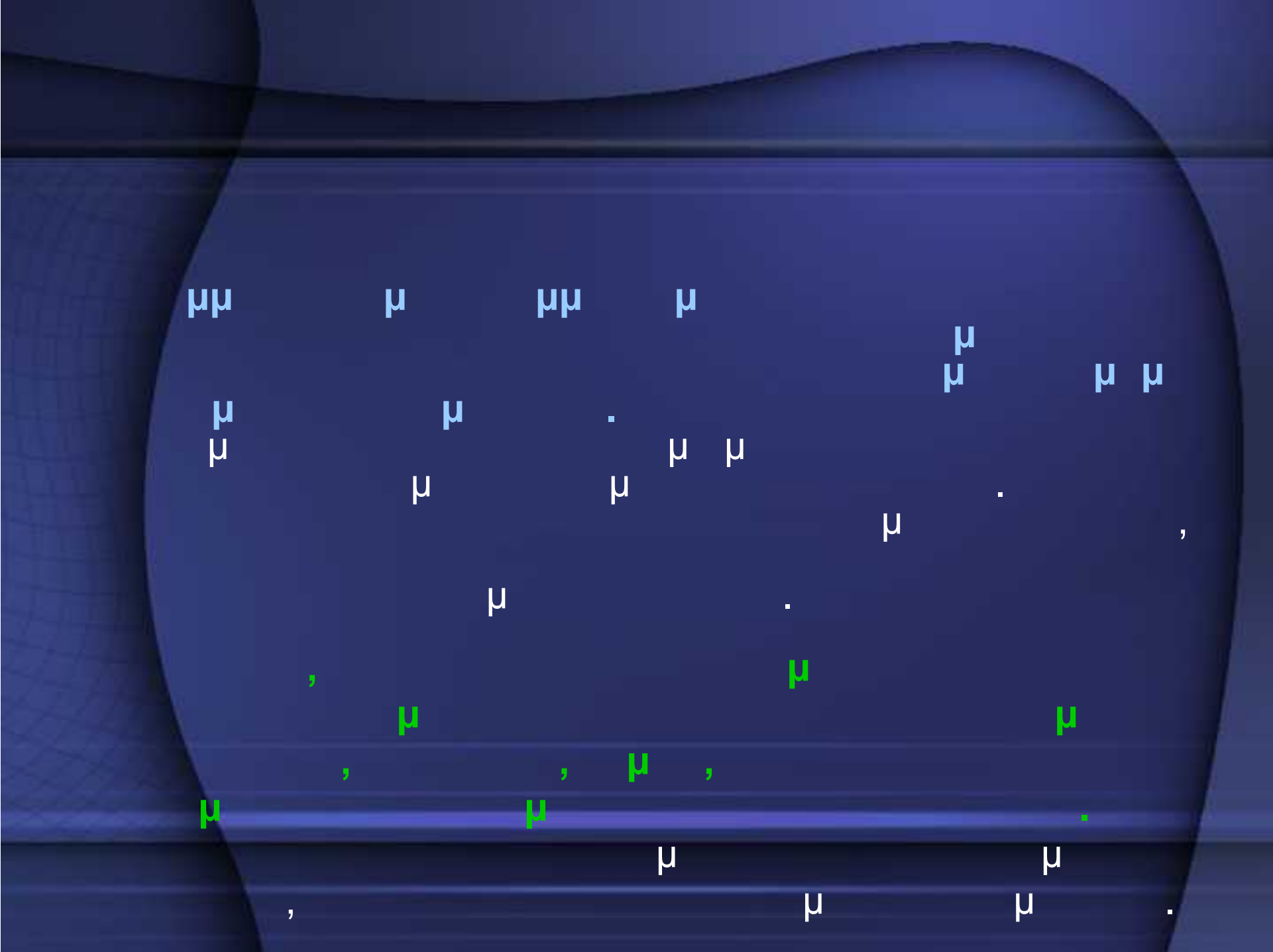
Σχήμα 7.1 Πλημμυρογραφήματα εισόδου $Q_A(t)$ και εξόδου $Q_B(t)$.



μ μ
 (Saint Venant). H
 μ μ
 μ μ
 μ (Chow, 1959,
 Henderson, 1966).
 $\mu\mu$ μ μ μ
 μ μ $D,$ μ μ
 $q_0,$ μ 50 $\mu\mu$ S_f
 μ μ $:$

$$\begin{aligned}
 V \frac{\partial y}{\partial x} + D \frac{\partial V}{\partial x} + \frac{\partial y}{\partial t} &= q_0 \\
 \frac{1}{g} \frac{\partial V}{\partial t} + \frac{\partial y}{\partial x} + \frac{V}{g} \frac{\partial V}{\partial x} &= S_0 - S_f
 \end{aligned}
 \tag{7.5}$$

μ , t :: μ
 $y(x,t), V(x,t)$ μ
 $(\mu, 1990)$



μ μ, μ
 $\mu \mu$ μ
 μ μ
McCarthy (1938) μ
 $:$

$$I - Q = dS / dt \quad (7.6)$$

- \bullet $Q =$ $\mu \mu$ $\mu - ,$
- \bullet $d_S/d_t = \mu$ $\mu \mu$
- \bullet μ μ

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7.2.

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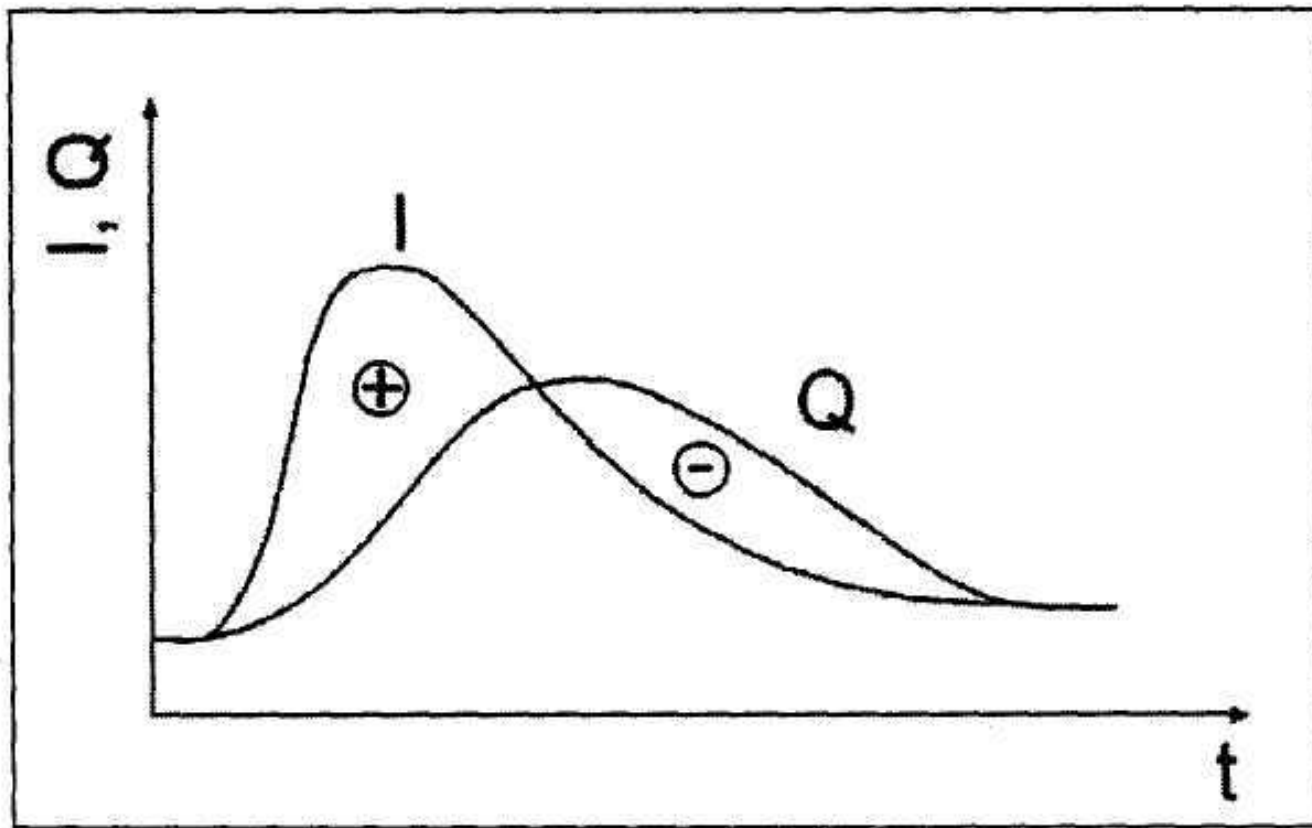
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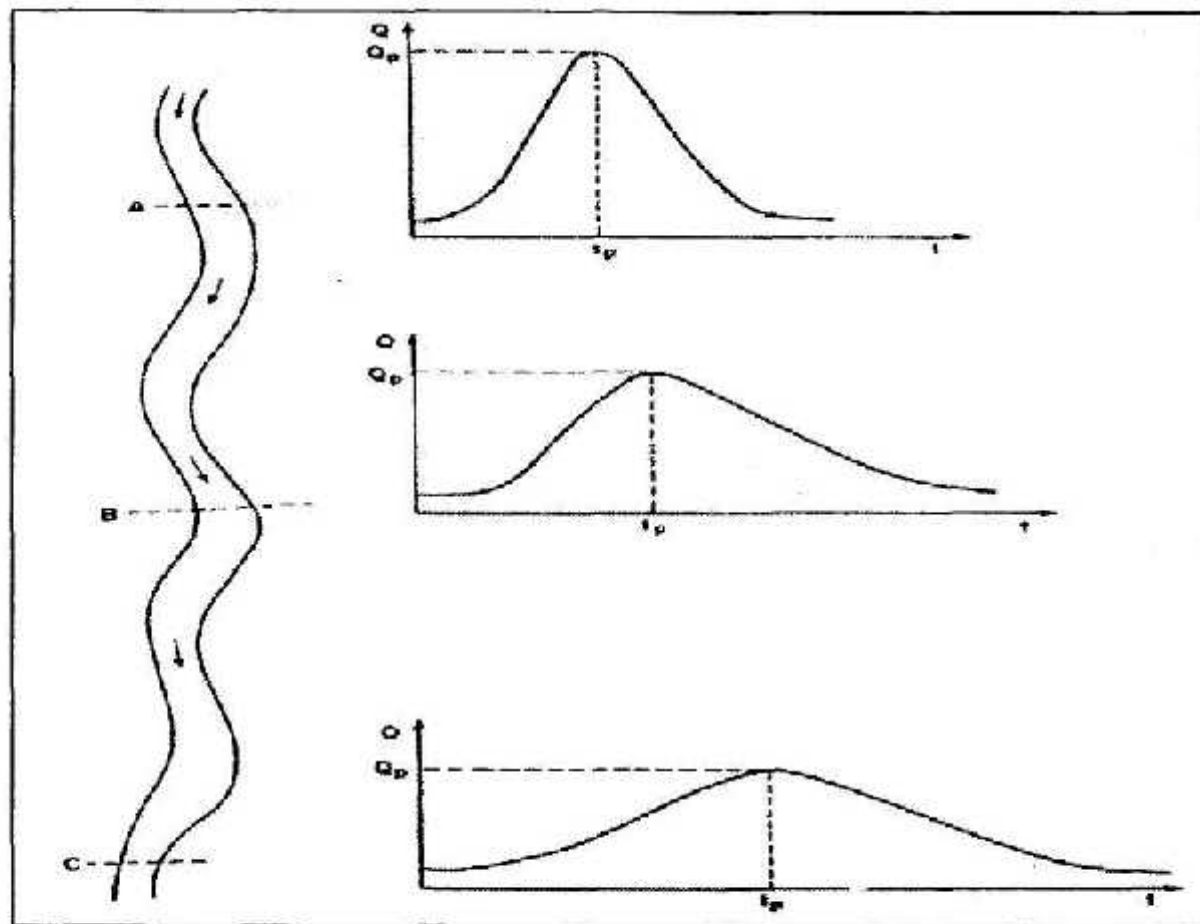
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Σχήμα 7.2 Μεταβολή ισοζυγίου εισροής και εκροής με το χρόνο.

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μ , μ μ μ μ μ
μ , μ μ μ μ μ
(μ
). μ μ μ μ
μ 7.3, μ μ
μ μ μ μ



Σχήμα 7.3 Το πλημμυρογράφημα στη θέση A, B και C όταν η πλευρική εισροή είναι μηδενική.

Q, μ

S μ μ $-$
 μ $:$

$$S = b(H - H_o)^m$$

(7.7)

$$Q = a(H - H_o)^n$$

(7.8)

:

▪ a, b, m n

$\mu\mu$

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▪ μ μ

▪ μ

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7.8

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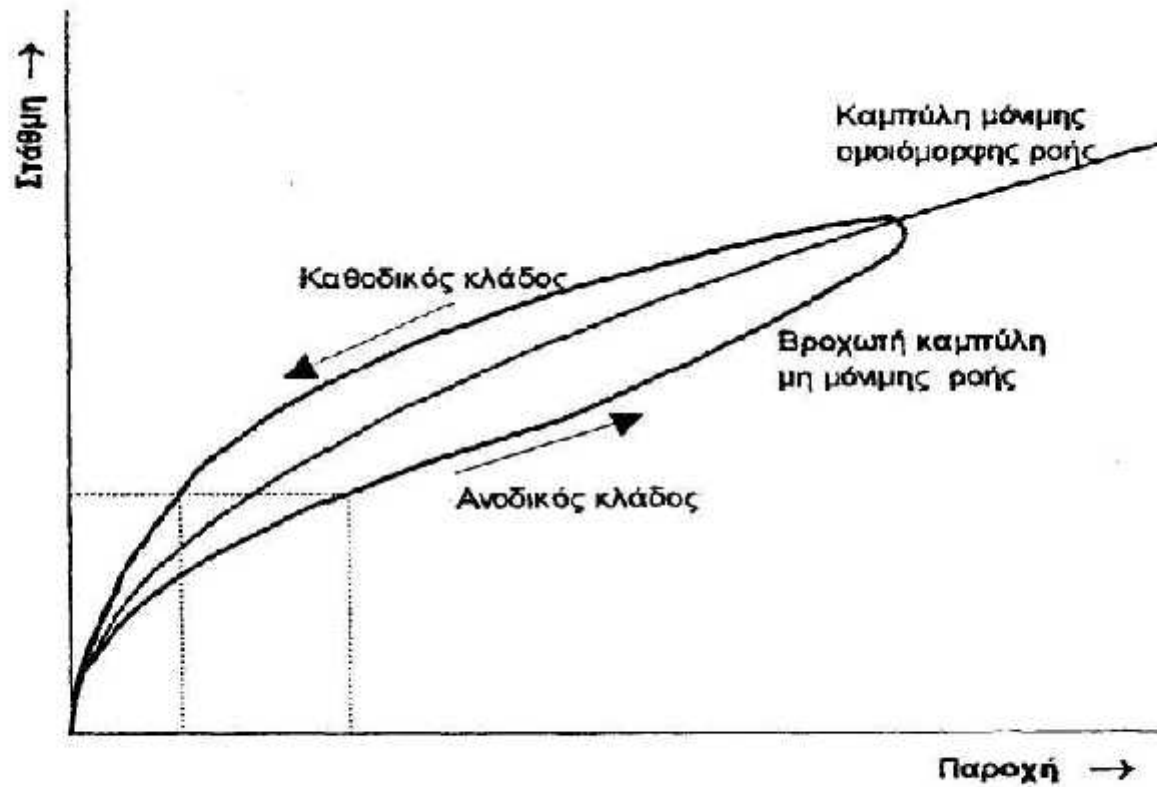
μ 7.4.

7.7

μ

S μ

Q.



Σχήμα 7.4 Σχέση ανάμεσα στη στάθμη και την παροχή.

$$S = \frac{b}{a} \left[xI^{m/n} + (1-x)Q^{m/n} \right]$$

(7.9)

b, a, m, n

7.7 7.8.

7.9

μ μ

μ

μ

μ

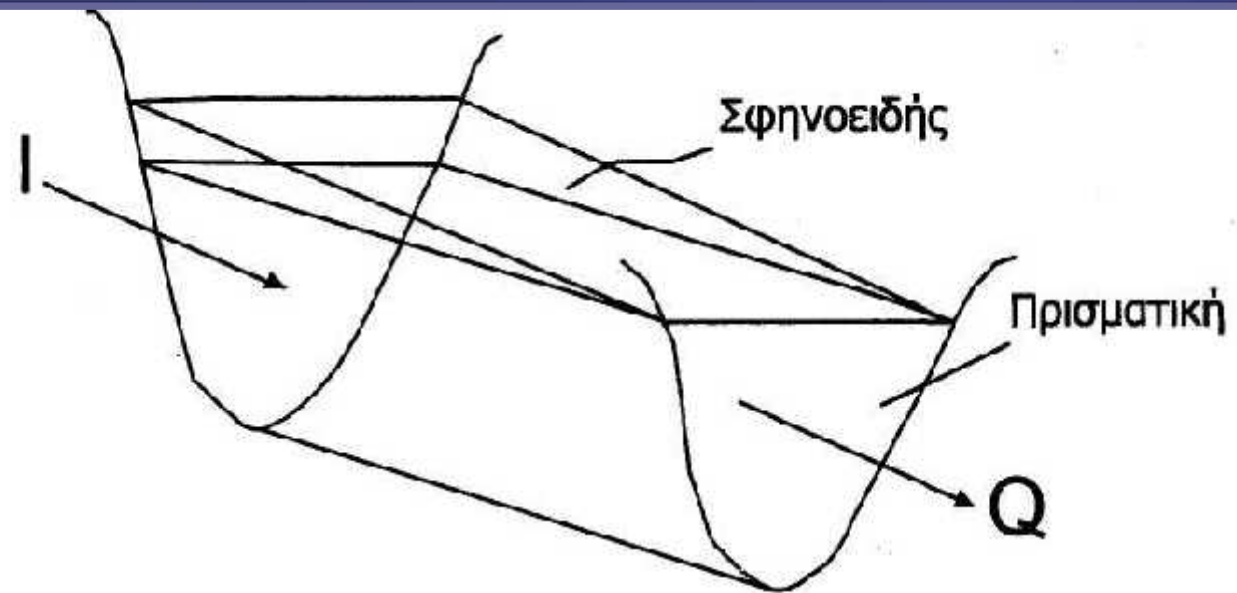
μ 7.5.

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Σχήμα 7.5 Διαχωρισμός αποθηκευτικότητας υδατορεύματος σε πρισματική και σφηνοειδή.

Muskingum

Muskingum

Muskingum

McCarthy (1938),

$$S_{ολ} = S_{\pi\rho\iota\sigma\mu} + S_{\sigma\phi\eta\nu} = KQ + Kx(I - Q) = K[xI + (1 - x)Q] \quad (7.10)$$

μ

μ μ

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μ

:

$$\bar{I} - \bar{Q} = \frac{\Delta S}{\Delta t} \Rightarrow \Delta S = (\bar{I} - \bar{Q})\Delta t \quad (7.11)$$

$$S_{j+1} - S_j = \frac{I_{j+1} + I_j}{2} \Delta t - \frac{Q_{j+1} + Q_j}{2} \Delta t \quad (7.12)$$

(7.10)

$S_{j+1} S_j$

:

$$S_{j+1} - S_j = K \{ (xI_{j+1} + (1-x)Q_{j+1}) - (xI_j + (1-x)Q_j) \} \quad (7.13)$$

(7.12)

(7.13)

μ

:

$$K \{ (xI_{j+1} + (1-x)Q_{j+1}) - (xI_j + (1-x)Q_j) \} = \frac{I_{j+1} + I_j}{2} \Delta t - \frac{Q_{j+1} + Q_j}{2} \Delta t \quad (7.14)$$

$$K = \frac{0.5\Delta t[(I_{j+1} + I_j) - (Q_{j+1} + Q_j)]}{(xI_{j+1} + (1-x)Q_{j+1}) - (xI_j + (1-x)Q_j)} \Rightarrow \quad (7.15)$$

$$K = \frac{0.5\Delta t[(I_{j+1} + I_j) - (Q_{j+1} + Q_j)]}{x(I_{j+1} - I_j) + (1-x)(Q_{j+1} - Q_j)}$$

Q_{j+1} μ μ
 Muskingum:

$$Q_{j+1} = C_0 I_{j+1} + C_1 I_j + C_2 Q_j \quad (7.16)$$

C_0, Q_1 C_2 :

$$C_0 = \frac{-Kx + 0.5\Delta t}{K - Kx + 0.5\Delta t} \quad (7.17)$$

$$C_1 = \frac{Kx + 0.5\Delta t}{K - Kx + 0.5\Delta t} \quad (7.18)$$

$$C_2 = \frac{K - Kx - 0.5\Delta t}{K - Kx + 0.5\Delta t} \quad (7.19)$$

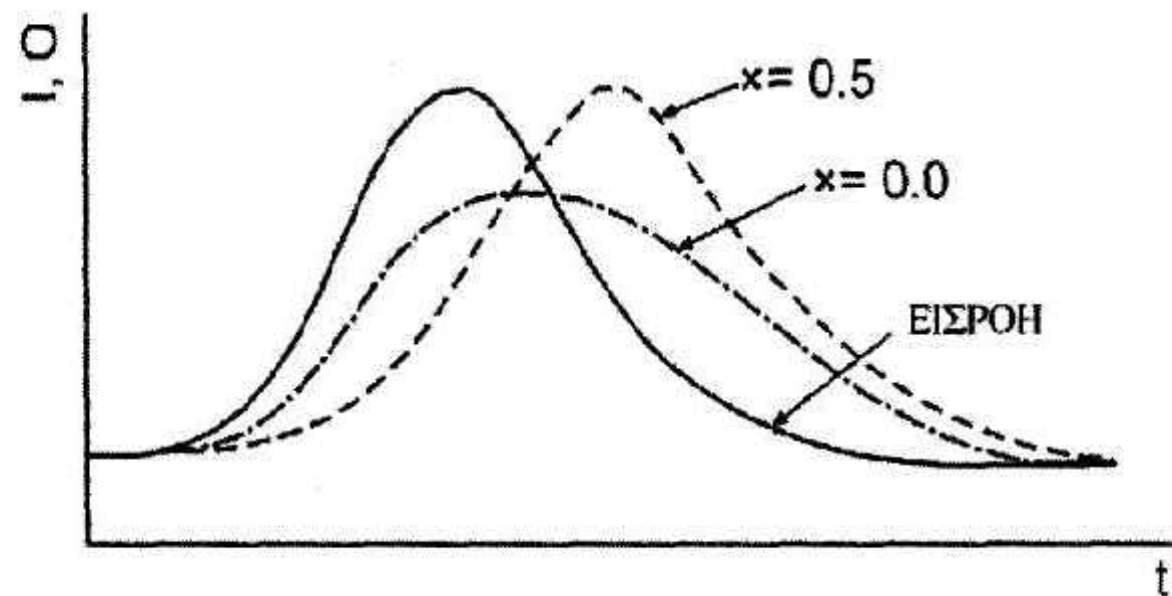
Muskingum

μ μ
 μ μ μ $j+1, \mu$
 μ μ μ j
 μ $j, j+1.$,
 μ μ μ ,
 $\mu\mu$.

C_0, Q_1 C_2 ,

μ .

μ
 $\mu\mu$
 μ μ μ
 $\mu\mu$ μ
 μ μ
 $\mu\mu$ μ μ μ
 μ $\mu\mu$ $0.5, \mu$ μ μ μ μ μ
 μ μ μ μ
 $\mu\mu$ μ μ $7.6.$ μ



Σχήμα 7.6 Διοδευμένα πλημμυρογραφήματα για χαρακτηριστικές τιμές του X .

μ Muskingum μ :

1. $\mu\mu$ μ
2. $\mu\mu$ μ (μ)
 $\mu\mu$ μ (μ)
 μ μ)

$$\mu : \mu \quad \mu$$

$$\mu \mu \quad S \quad \mu \quad \mu$$

$$: \quad [xI + (1-x)Q], \quad \mu \quad \mu$$

$$S = K[xI + (1-x)Q]$$

(7.20)

$$\mu \quad \mu \quad S \quad \mu$$

$$\mu \quad \mu \quad \mu \quad \mu \quad \mu \quad \mu$$

$$\mu \quad \mu \quad \mu \quad \mu \quad \mu \quad \mu$$

$$I - Q = \frac{dS}{dt} \Rightarrow S_{j+1} - S_j = \Delta t \left[\frac{I_j + I_{j+1}}{2} - \frac{Q_j + Q_{j+1}}{2} \right]$$

(7.21)

$\mu\mu \quad \mu$

$\mu \quad \mu$

:

1. $(Q_{j+1} + Q_j)/2 \quad \mu \quad \mu \quad \mu \quad (l_j+1+l_j)/2$

2. $\mu \quad \mu \quad \mu \quad S$

($\mu, \mu \quad 7.20) \quad xl+(1-x)Q$

3. $S \quad \mu \quad \mu \quad xl+(1-x)Q$

4. $\mu \quad \mu \quad \mu$

$\mu\mu, \quad \mu \quad [xl+(1-x)Q, S]$

5. $\mu \quad S \quad \mu$

7.3.2

MUSKINGUM CREST SEGMENT

$$Q_n = C_0 I_n + C_1 I_{n-1} + C_2 Q_{n-1} \quad (7.16)$$

$$Q_n = C_0 I_n + C_1 I_{n-1} + C_2 Q_{n-1} \quad (7.23)$$

$$Q_{n-1} = C_0 I_{n-1} + C_1 I_{n-2} + C_2 Q_{n-2} \quad (7.24)$$

$$Q_n = K_1 I_n + K_2 I_{n-1} + K_3 I_{n-2} + \dots + K_n I_1 \quad (7.25)$$

$$K_1 = C_0$$

$$K_2 = C_0 C_2 + C_1$$

$$K_3 = K_2 C_2$$

$$K_i = K_{i-1} C_2 \text{ για } i > 2$$

μ μ
 $Q_n,$

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Muskingum.

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7.3.3

SCS CONVEX

Conservation Service) Muskingum
 7.10
 SCS (Soil Conservation Service) Muskingum
 Q_1
 $I_1 - Q_1$
 Q_2
 t
 Q_1
 $I_1 - Q_1$
 Q_2
 t

$$Q_2 = Q_1 + C_t(I_1 - Q_1)$$

(7.26)

(7.26)

μ Q : μ μ μ μ .

$$C_t = \frac{Q_2 - Q_1}{I_1 - Q_1}$$

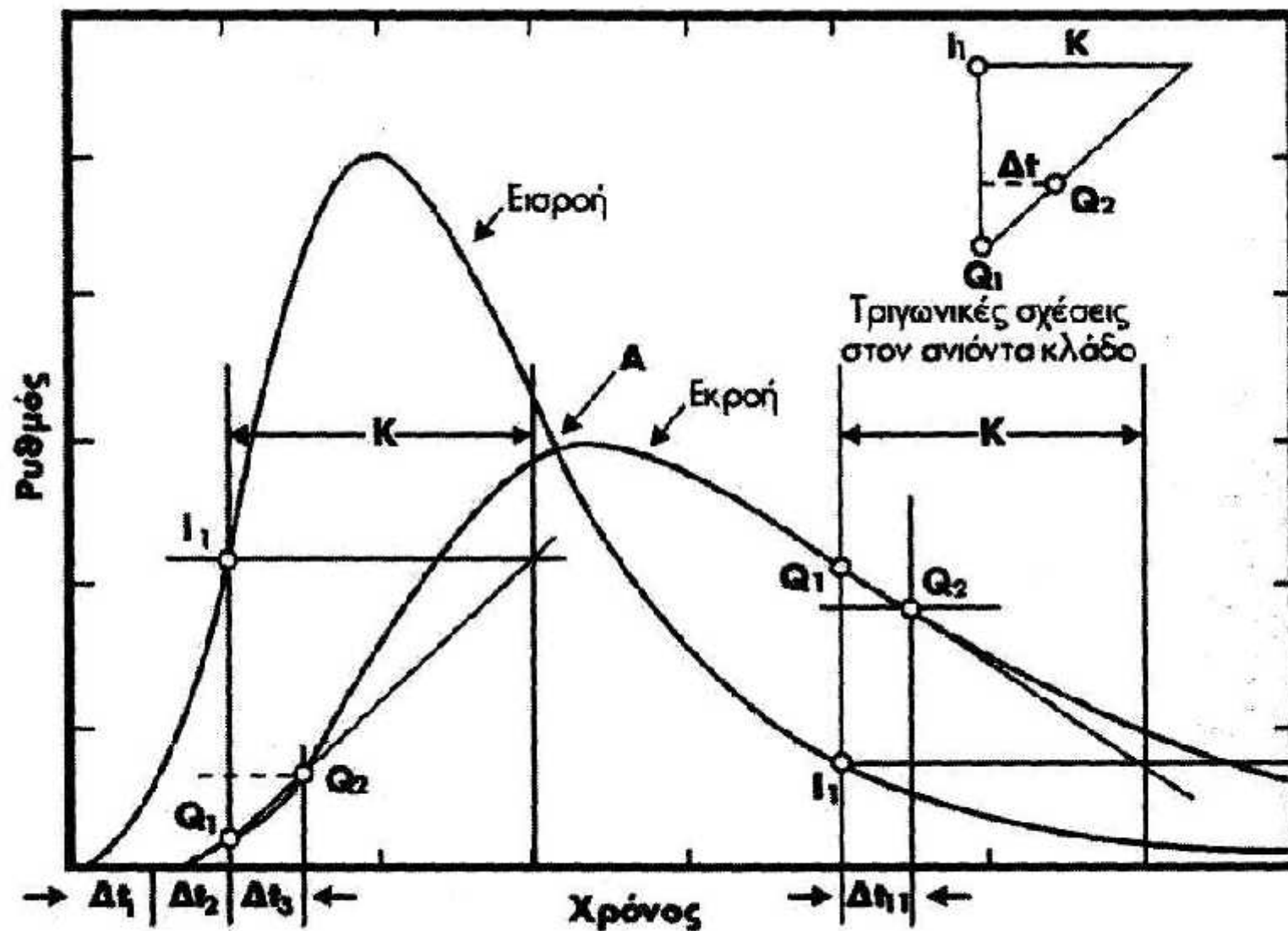
(7.27)

μ , :

$$\frac{\Delta_t}{K} = \frac{Q_2 - Q_1}{I_1 - Q_1}$$

(7.28)

μ Q_1 Q_2 μ μ



Σχήμα 7.10 Γεωμετρικές σχέσεις που χρησιμοποιήθηκαν στην SCS μέθοδο διόδευσης.

$$C_t = \frac{V}{V+1.7} \quad (7.30)$$

V
 $V+1.7$
 (Viessman and Lewis, 1995).
 (7.30)
 Convex SCS
 Q_2
 2.
 .

7.3.4

MUSKINGUM - CUNGE

Cunge

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Muskingum μ

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$$\frac{dS}{dt} = \bar{I} - \bar{Q} \Rightarrow K \frac{d}{dt} [xI + (1-x)Q] = \bar{I} - \bar{Q} \quad (7.31)$$

μ

:

$\mu Q_i,$

$Q \mu Q_{i+1}$

$$\frac{K}{\Delta t} [xQ_i^{t+1} + (1-x)Q_{i+1}^{t+1} - xQ_i^t - (1-x)Q_{i+1}^t] = \frac{1}{2} (Q_i^{t+1} - Q_{i+1}^{t+1} + Q_i^t - Q_{i+1}^t)$$

(7.32)

$$\frac{\partial Q}{\partial t} + c \frac{\partial Q}{\partial x} = 0 \quad (7.32)$$

$$\frac{\partial Q}{\partial t} + c \frac{\partial Q}{\partial x} = 0 \quad (7.33)$$

(7.32)

Muskingum-Cunge:

$$Q_{i+1}^{t+1} = C_0 Q_i^{t+1} + C_1 Q_i^t + C_2 Q_{i+1}^t \quad (7.34)$$

$$C_0 = \frac{\Delta t / K - 2X}{2(1-x) + \Delta t / K} \quad (7.35)$$

$$C_1 = \frac{\Delta t / K + 2X}{2(1-x) + \Delta t / K} \quad (7.36)$$

$$C_2 = \frac{2(1-x) - c\Delta t / \Delta x}{2(1-x) + \Delta t / K} \quad (7.37)$$

C_0, C_1, C_2

μ

μ :

$$x = \frac{1}{2} \left(1 - \frac{q_0}{S_0 c \Delta x} \right) \quad (7.38)$$

: $S_0 =$ μ
 $q_0 =$

μ $\mu\mu$ μ c :

$$c = m V \quad (7.39)$$

V μ m μ $5/3$ μ

μ . m

μ μ :

$$Q = b A^m \quad (7.40)$$

7.4

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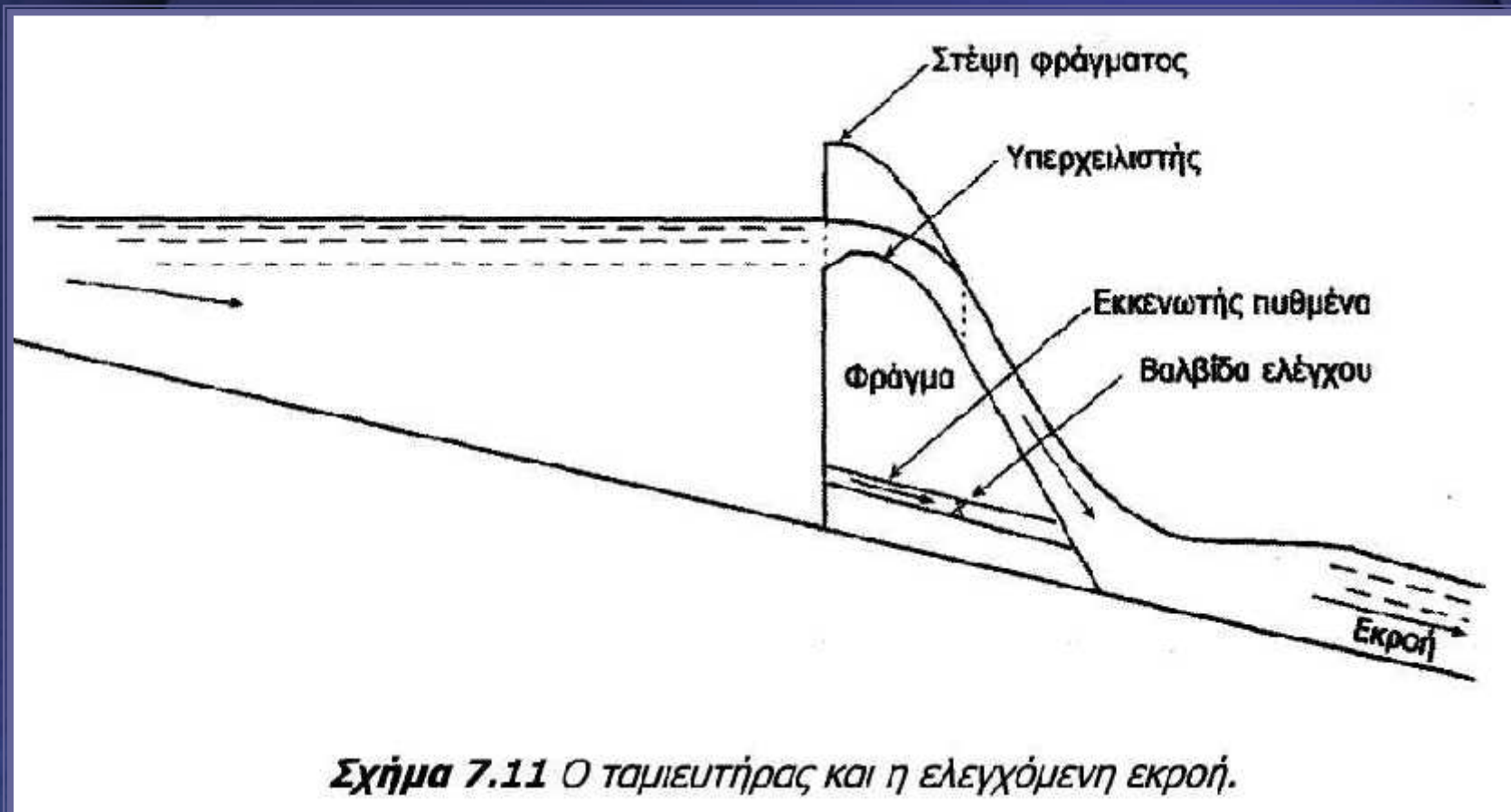
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$$\frac{\Delta S}{\Delta t} = I(t) \quad (7.41)$$

$$\frac{\Delta S}{\Delta t} = I(t) - Q(t) \Rightarrow \frac{S_{n+1} - S_n}{\Delta t} = \frac{I_n + I_{n+1}}{2} - \frac{Q_n + Q_{n+1}}{2} \Rightarrow$$

$$\frac{2(S_{n+1} - S_n)}{\Delta t} = (I_n + I_{n+1}) - (Q_{n+1} + Q_n) \Rightarrow$$

$$\left(\frac{2S_{n+1}}{\Delta t} + Q_{n+1} \right) = (I_{n+1} + I_n) + \left(\frac{2S_n}{\Delta t} - Q_n \right)$$

(7.42)

$n, n+1$

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$n, n+1$

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$n,$

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$, \mu$

(7.42)

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μ

μ

S_{n+1}

Q_{n+1}

(

μ

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) S_n

Q_n .

$$Q = CY(H - H_0)^x$$

(7.43)

Q =
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C =
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(μ 3)
μ 3/2

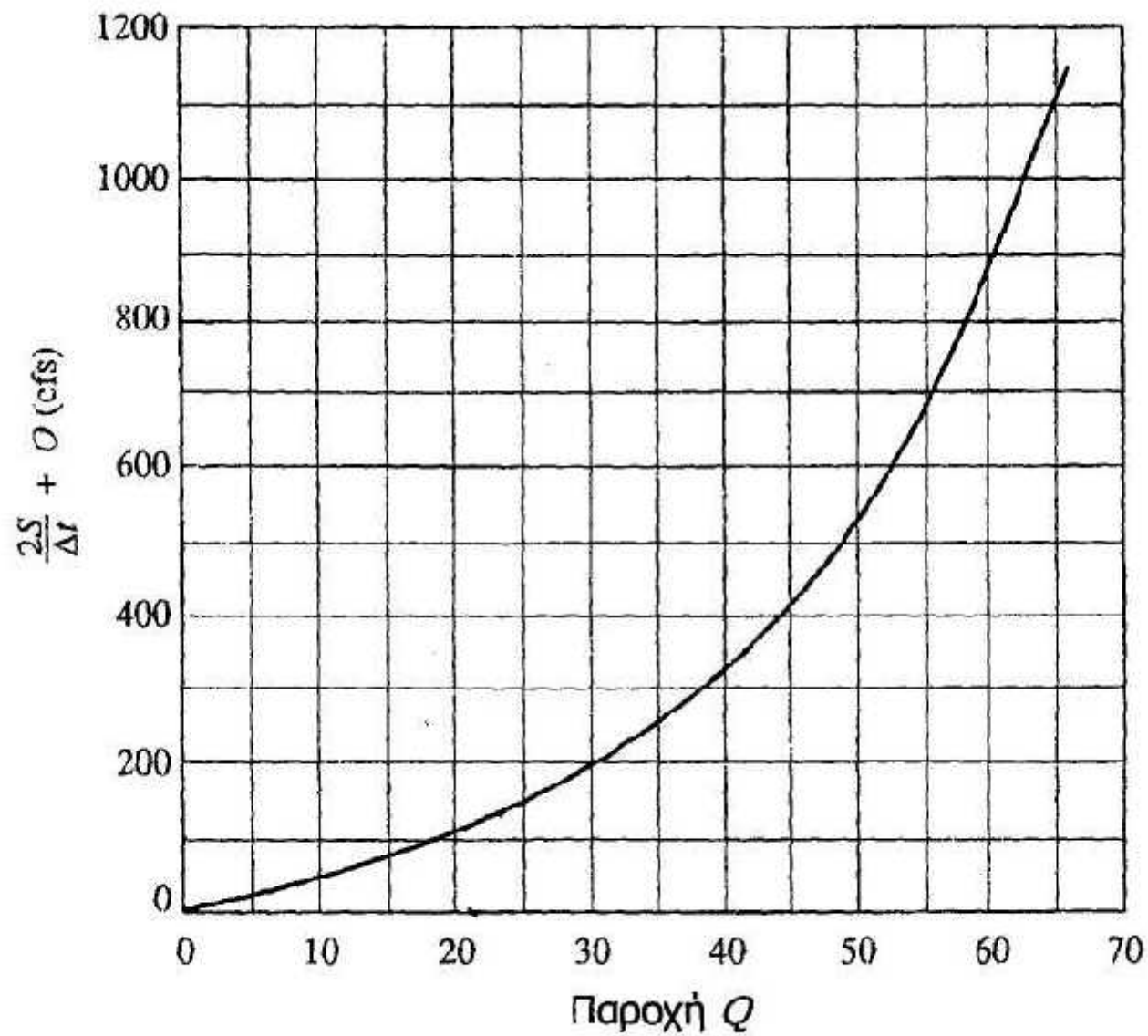
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μ μ μ , μ μ
S, μ Q, μ μ Q
μ μ μ μ Q
) μ (μ μ :
μ μ μ μ

7.43

$$Q = CY(H - H_0)^{3/2}$$

$$: \left(\frac{2S}{\Delta t} + Q, Q \right) \quad Q = f \left(\frac{2S}{\Delta t} + Q \right)$$

7.12.



Σχήμα 7.12 Σχέση παροχής Q και $2S/\Delta t + Q$.

μ
 Modified Puls method.

$$(7.42) \quad \mu \mu \quad ,$$

Storage indication

$$\mu \quad \mu \quad :$$

$\mu \quad n=1,$
 $\mu \mu \quad , \mu \quad S_n = 0 \quad Q_n = 0.$
 (7.42)
 $\mu \quad n+1=2, \quad :$

$$\left(\frac{2S_2}{\Delta t} + Q_2\right) = (I_2 + I_1) + \left(\frac{2S_1}{\Delta t} - Q_1\right) = (I_2 + I_1) + 0 = (I_2 + I_1) \quad (7.45)$$

μ :
 $\left(\frac{2S_2}{\Delta t} + Q_2 \right)$

$$Q = f \left(\frac{2S}{\Delta t} + Q \right)$$

μ μ Q₂ μ μ μ
μ μ μ , μ μ
μ μ .

$$\begin{aligned}
 & \left(\frac{2S_2}{\Delta t} + Q_2 \right) \\
 & : \\
 & \left(\frac{2S_n}{\Delta t} - Q_n \right) = \left(\frac{2S_n}{\Delta t} + Q_n \right) - 2Q_n
 \end{aligned}$$

$n=2, \dots, n=3,$

$(7.44).$